

CSCI 420 Computer Graphics

Lecture 15

Ray Tracing

Ray Casting

Shadow Rays

Reflection and Transmission

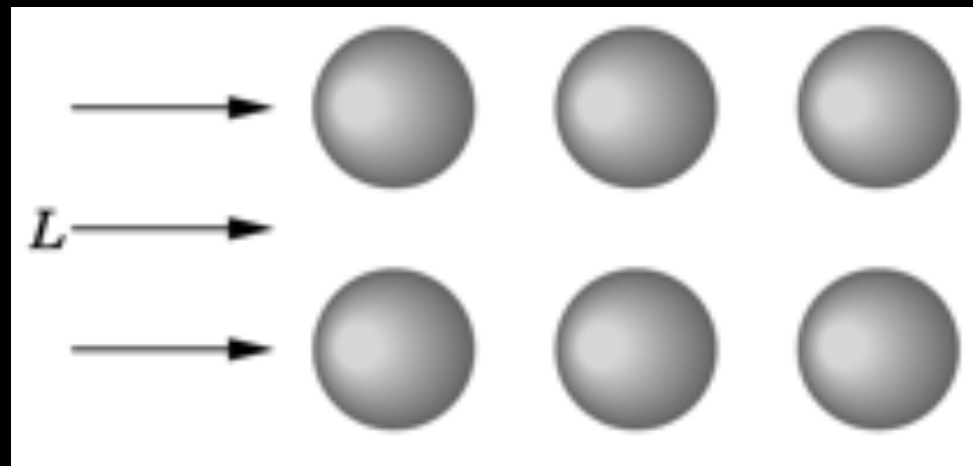
[Ch. 13.2 - 13.3]

Jernej Barbic

University of Southern California

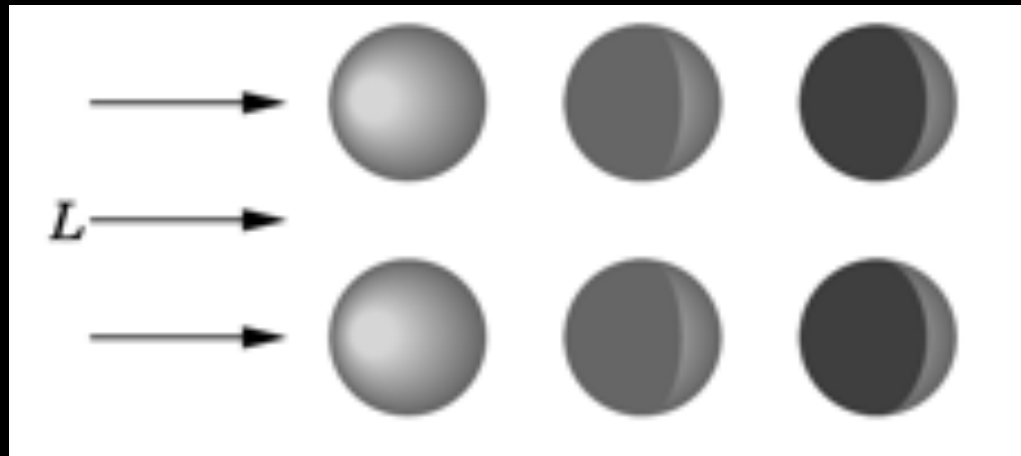
Local Illumination

- Object illuminations are independent
- No light scattering between objects
- No real shadows, reflection, transmission
- OpenGL pipeline uses this



Global Illumination

- Ray tracing (highlights, reflection, transmission)
- Radiosity (surface interreflections)
- Photon mapping
- Precomputed Radiance Transfer (PRT)



Object Space:

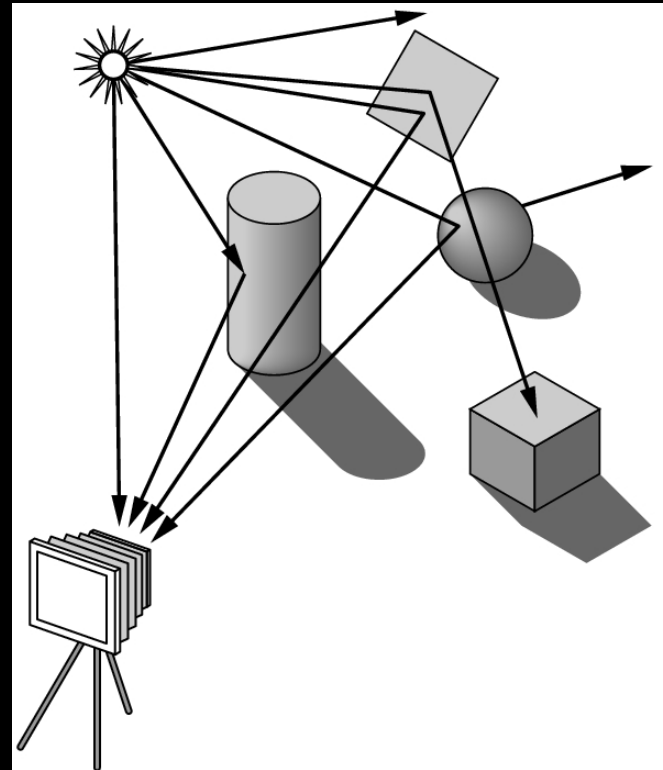
- Graphics pipeline: **for each object**, render
 - Efficient pipeline architecture, real-time
 - Difficulty: object interactions (shadows, reflections, etc.)

Image Space:

- Ray tracing: **for each pixel**, determine color
 - Pixel-level parallelism
 - Difficulty: very intensive computation, usually off-line

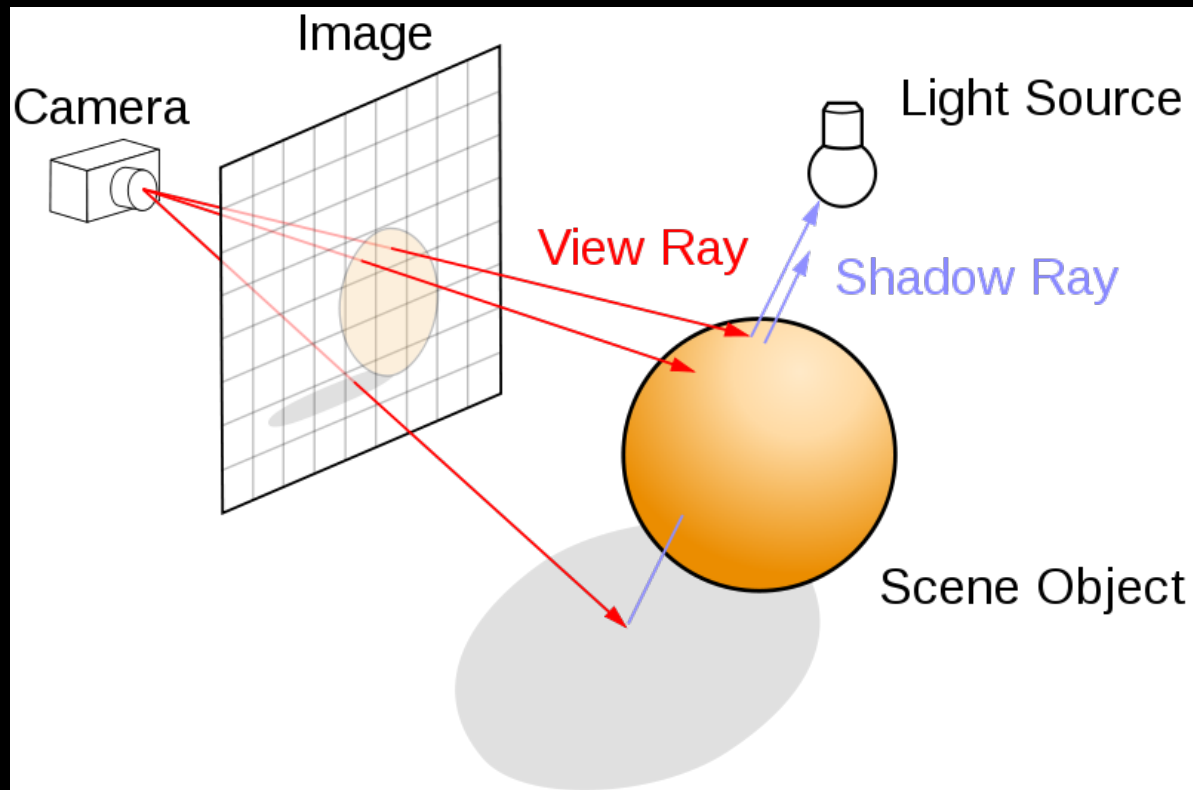
First idea: Forward Ray Tracing

- Shoot (many) light rays from each light source
- Rays bounce off the objects
- Simulates paths of photons
- Problem: many rays will miss camera and not contribute to image!
- This algorithm is not practical



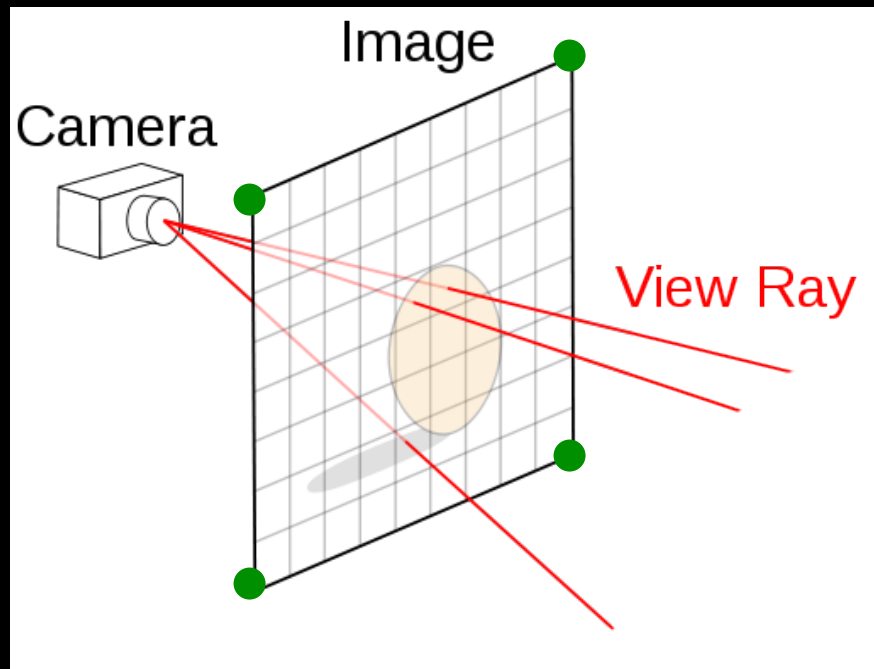
Backward Ray Tracing

- Shoot one ray from camera through each pixel in image plane



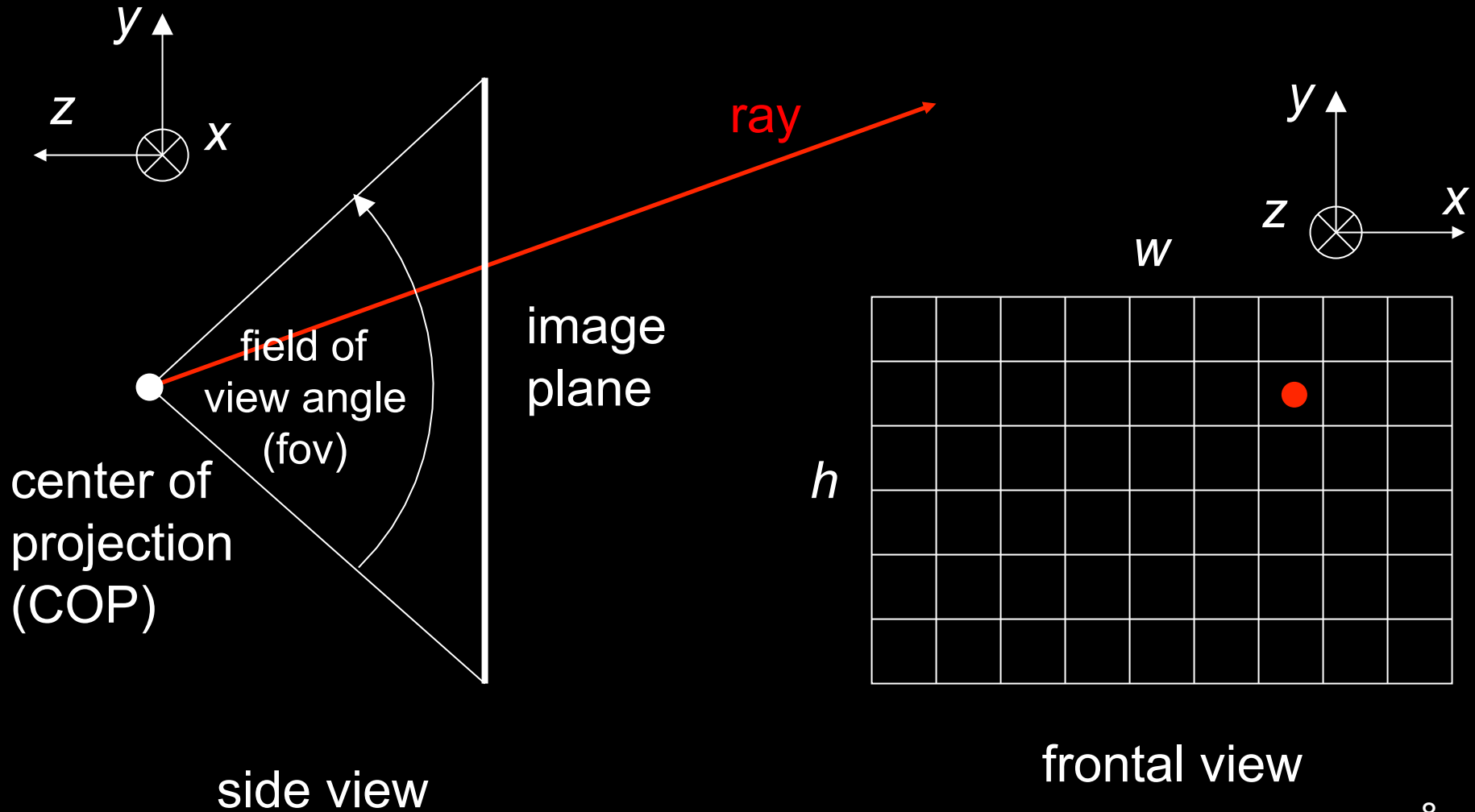
Generating Rays

- Camera is at $(0,0,0)$ and points in the negative z-direction
- Must determine coordinates of image corners in 3D

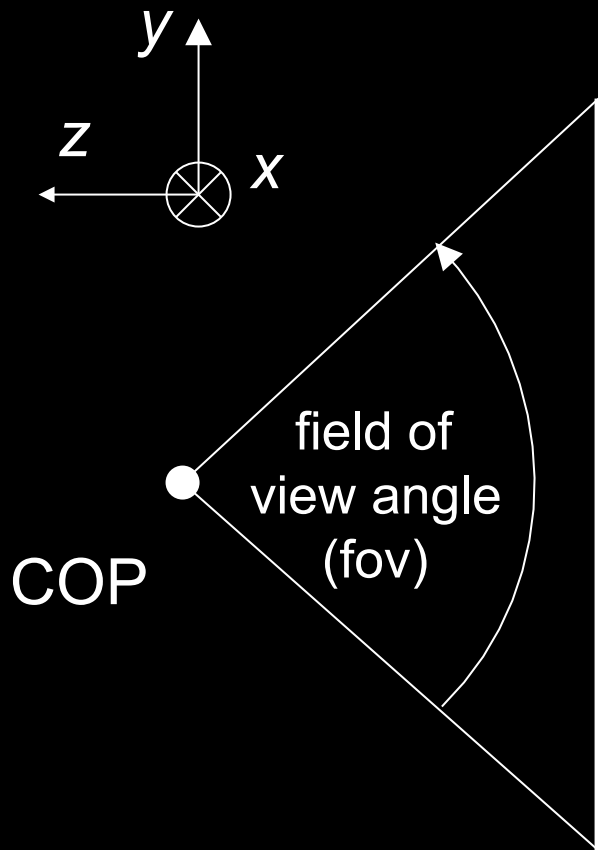


Generating Rays

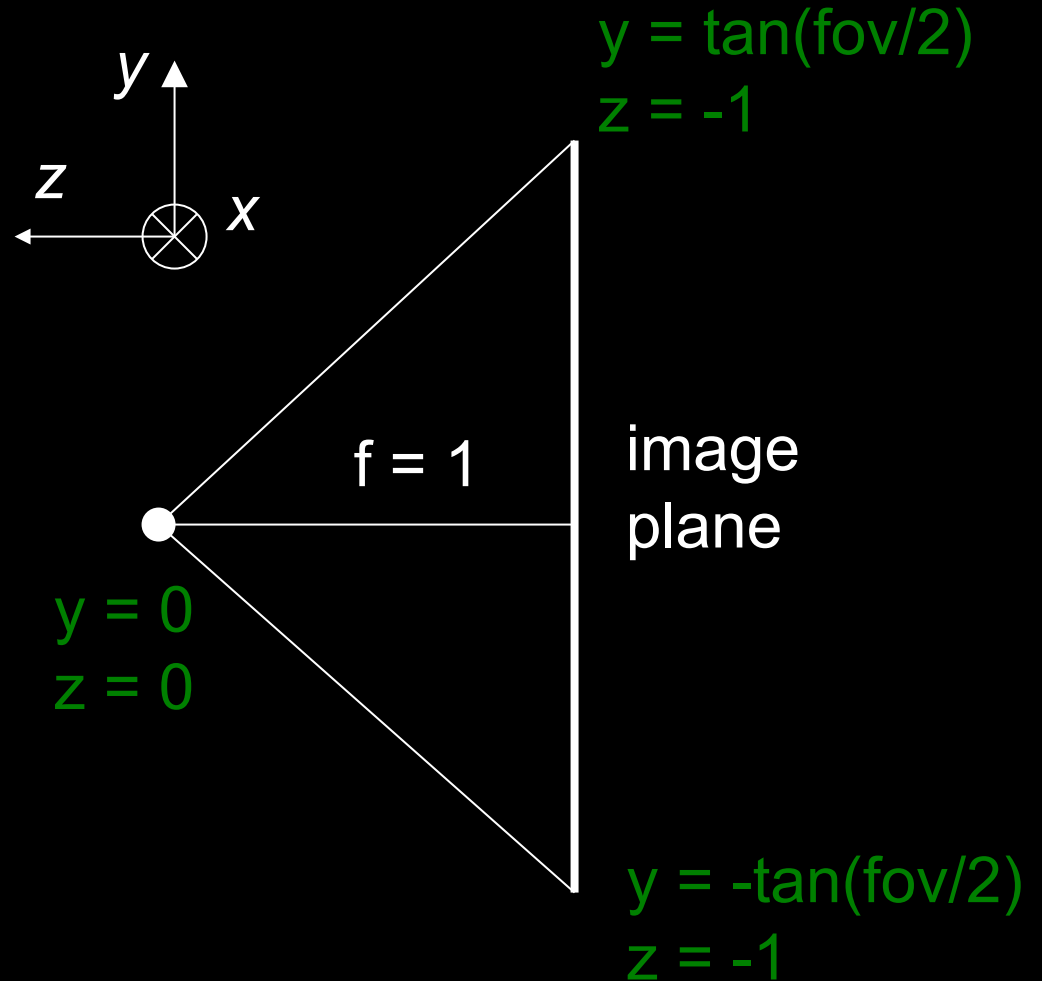
$$\text{aspect ratio} = w / h$$



Generating Rays

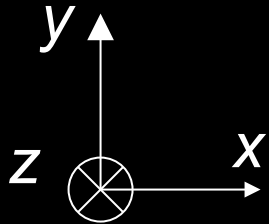


side view



side view

Generating Rays

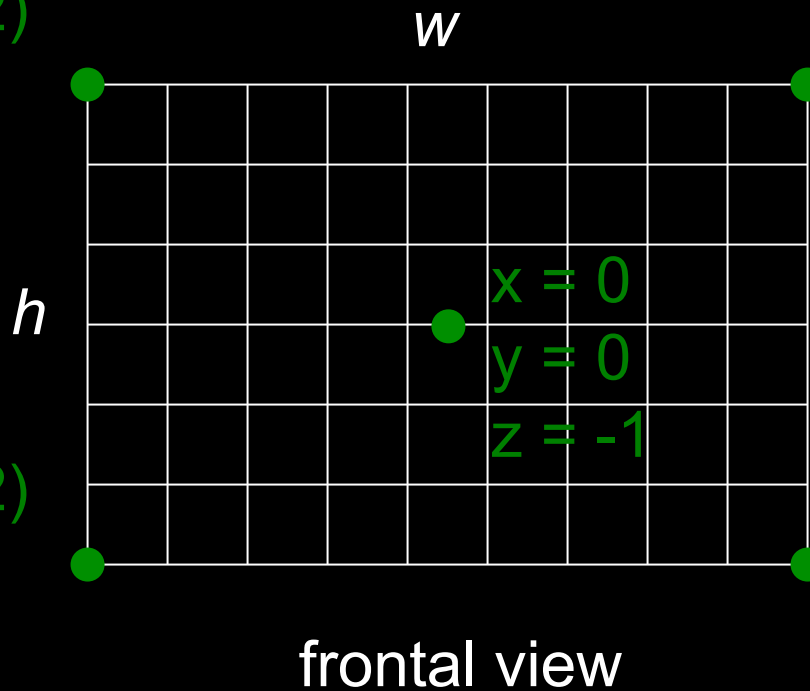


$a = \text{aspect ratio} = w / h$

$$\begin{aligned}x &= -a \tan(\text{fov}/2) \\y &= \tan(\text{fov}/2) \\z &= -1\end{aligned}$$

$$\begin{aligned}x &= a \tan(\text{fov}/2) \\y &= \tan(\text{fov}/2) \\z &= -1\end{aligned}$$

$$\begin{aligned}x &= -a \tan(\text{fov}/2) \\y &= -\tan(\text{fov}/2) \\z &= -1\end{aligned}$$

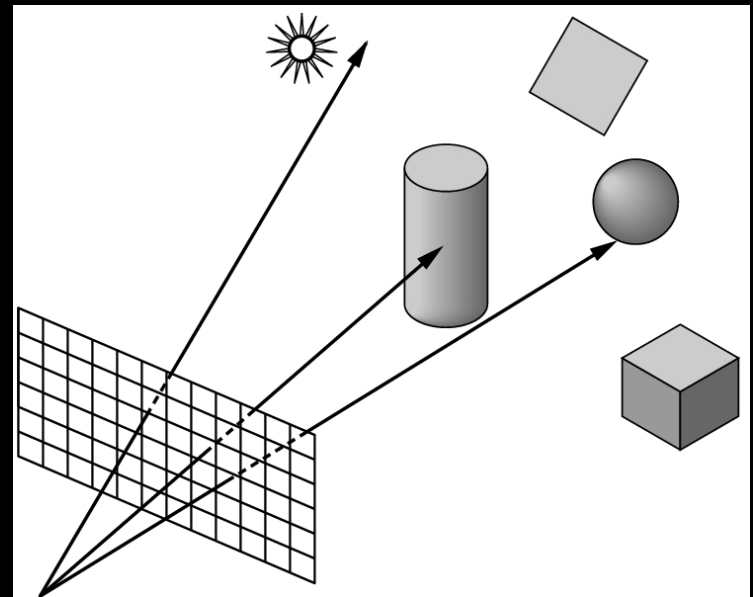


$$\begin{aligned}x &= a \tan(\text{fov}/2) \\y &= -\tan(\text{fov}/2) \\z &= -1\end{aligned}$$

Determining Pixel Color

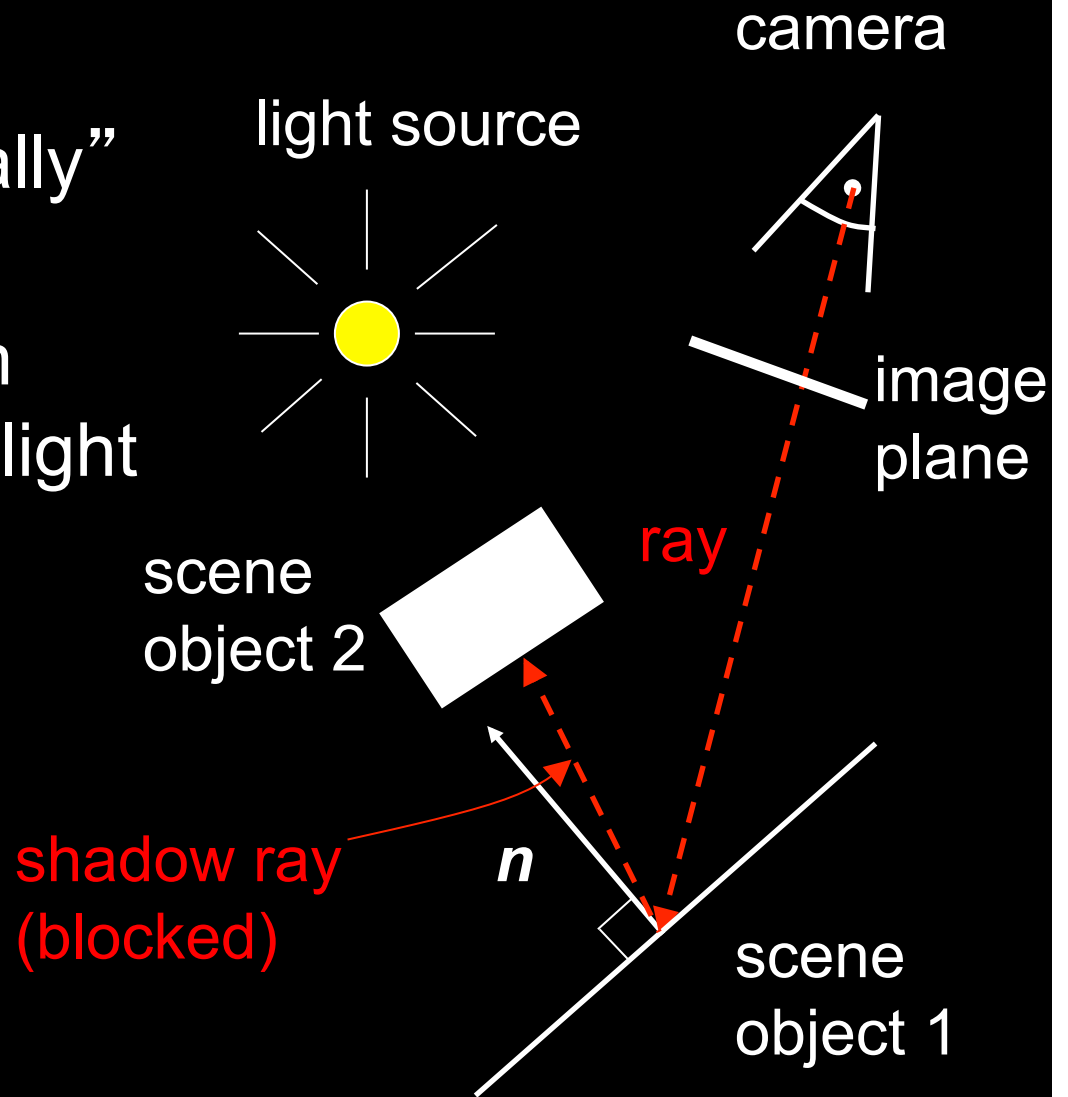
1. Phong model (local as before)
2. Shadow rays
3. Specular reflection
4. Specular transmission

Steps (3) and (4) require recursion.



Shadow Rays

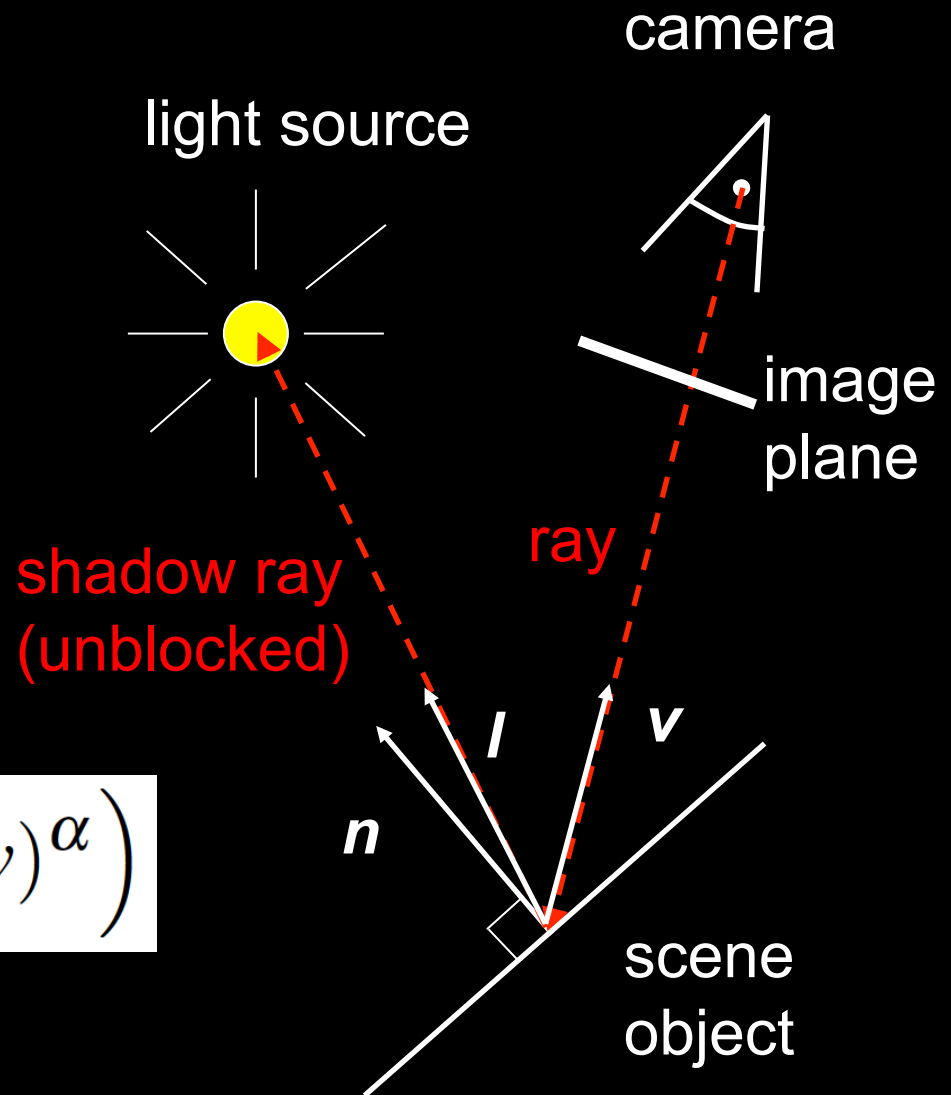
- Determine if light “really” hits surface point
- Cast **shadow ray** from surface point to each light
- If shadow ray hits opaque object, no contribution from that light
- This is essentially improved diffuse reflection



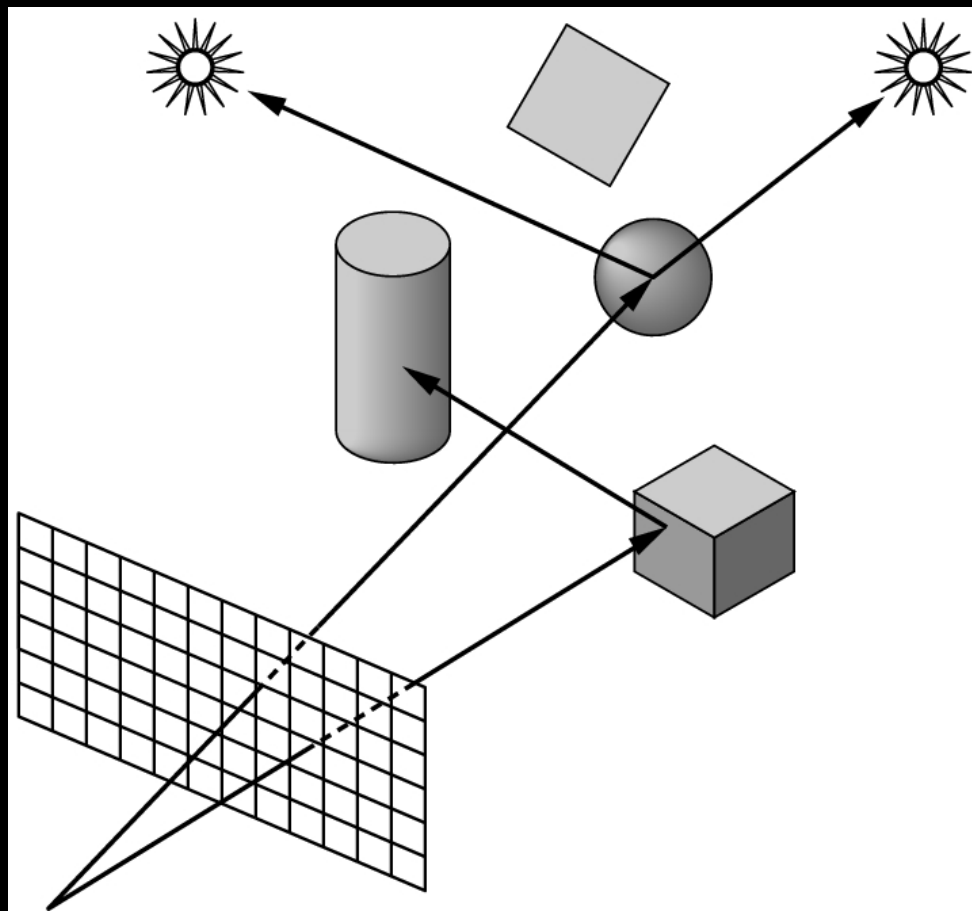
Phong Model

- If shadow ray can reach to the light, apply a standard Phong model

$$I = L \left(k_d (l \cdot n) + k_s (r \cdot v)^\alpha \right)$$

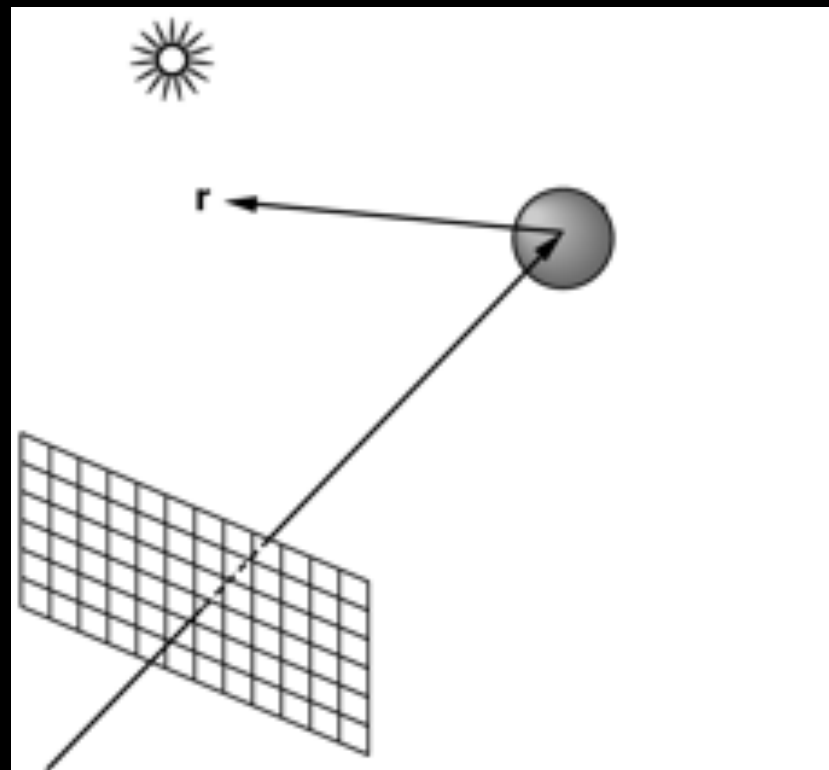


Where is Phong model applied
in this example?
Which shadow rays are blocked?



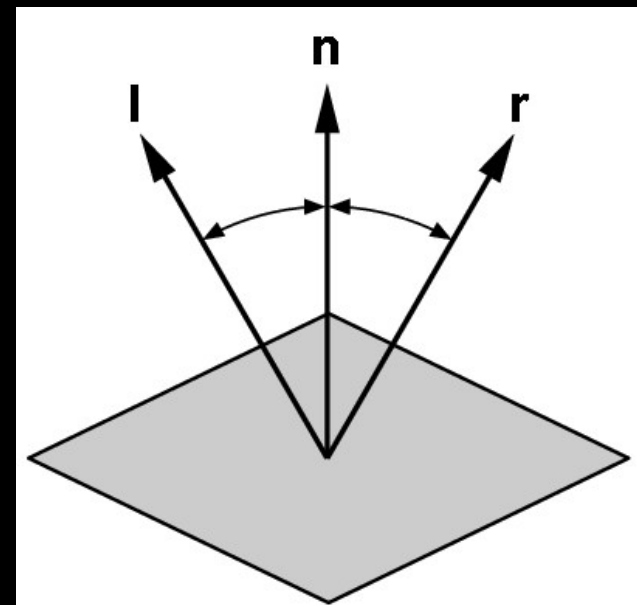
Reflection Rays

- For specular component of illumination
- Compute **reflection ray** (recall: backward!)
- Call ray tracer recursively to determine color

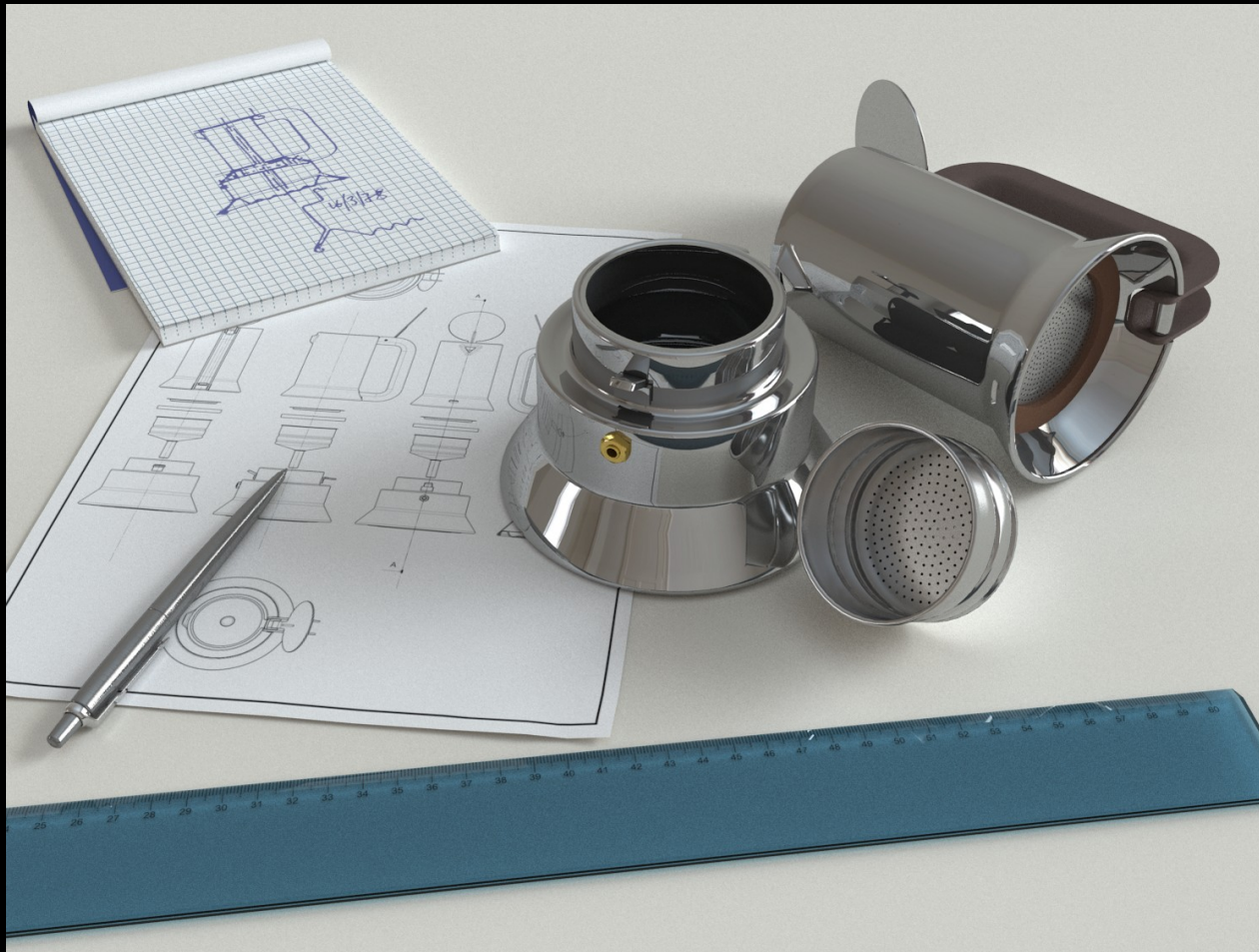


Angle of Reflection

- Recall: incoming angle = outgoing angle
- $\mathbf{r} = 2(\mathbf{l} \cdot \mathbf{n}) \mathbf{n} - \mathbf{l}$
- Compute only for surfaces that are reflective



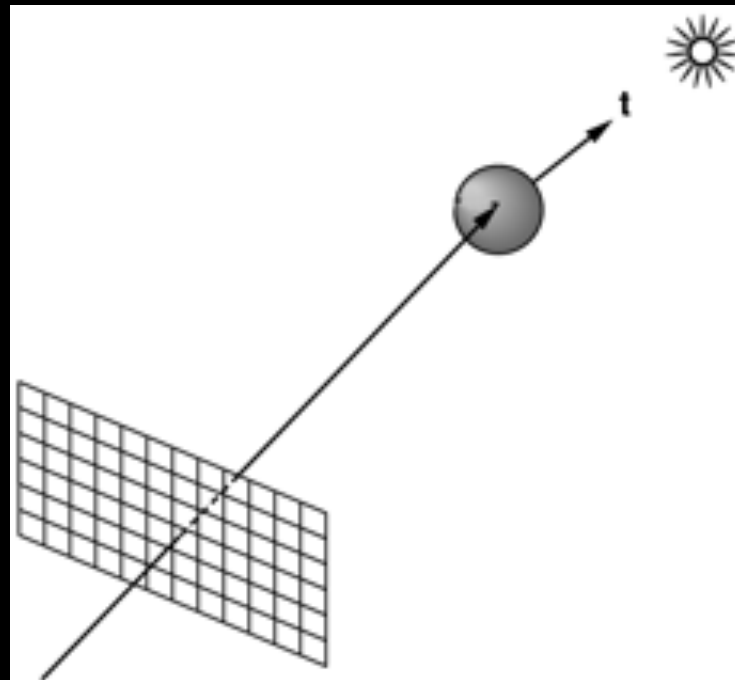
Reflections Example



www.yafaray.org

Transmission Rays

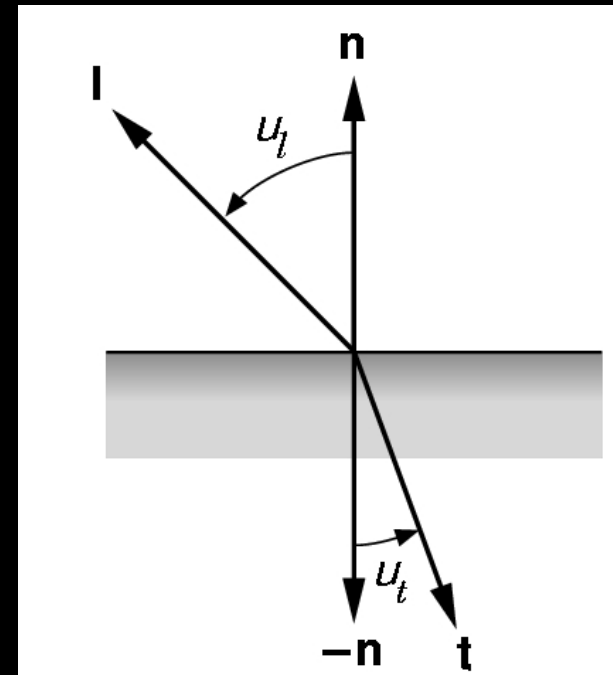
- Calculate light transmitted through surfaces
- Example: water, glass
- Compute **transmission ray**
- Call ray tracer recursively to determine color



Transmitted Light

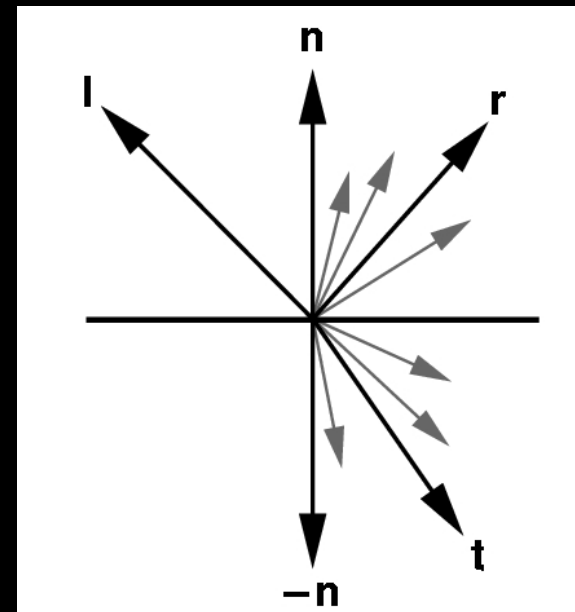
- Index of refraction is speed of light, relative to speed of light in vacuum
 - Vacuum: 1.0 (per definition)
 - Air: 1.000277 (approximate to 1.0)
 - Water: 1.33
 - Glass: 1.49
- Compute t using Snell's law
 - η_l = index for upper material
 - η_t = index for lower material

$$\frac{\sin(u_l)}{\sin(u_t)} = \frac{\eta_t}{\eta_l} = \eta$$



Translucency

- Most real objects are not transparent, but blur the background image
- Scatter light on other side of surface
- Use stochastic sampling (called distributed ray tracing)



Transmission + Translucency Example



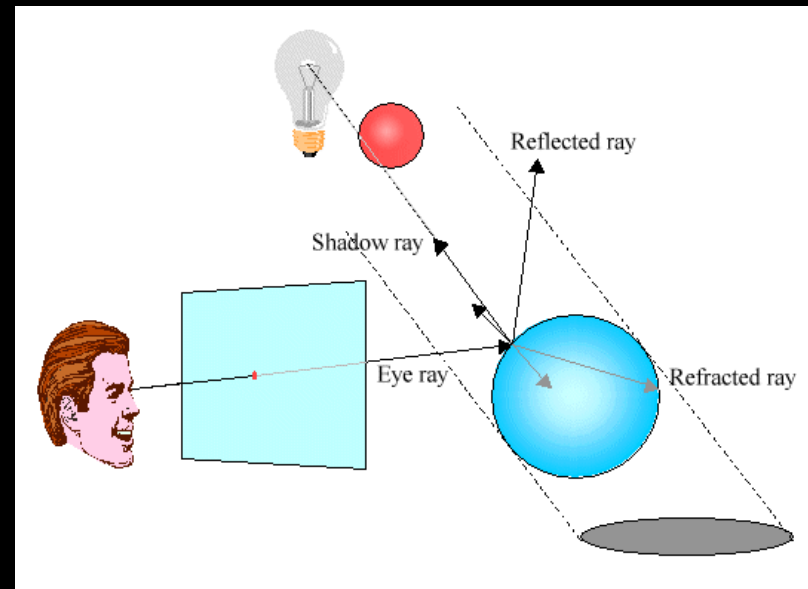
www.povray.org

The Ray Casting Algorithm

- Simplest case of ray tracing
 1. For each pixel (x,y) , fire a ray from COP through (x,y)
 2. For each ray & object, calculate closest intersection
 3. For closest intersection point p
 - Calculate surface normal
 - For each light source, fire shadow ray
 - For each unblocked shadow ray, evaluate local Phong model for that light, and add the result to pixel color
- Critical operations
 - Ray-surface intersections
 - Illumination calculation

Recursive Ray Tracing

- Also calculate specular component
 - Reflect ray from eye on specular surface
 - Transmit ray from eye through transparent surface
- Determine color of incoming ray by recursion
- Trace to fixed depth
- Cut off if contribution below threshold



Ray Tracing Assessment

- Global illumination method
- Image-based
- Pluses
 - Relatively accurate shadows, reflections, refractions
- Minuses
 - Slow (per pixel parallelism, not pipeline parallelism)
 - Aliasing
 - Inter-object diffuse reflections require many bounces

Raytracing Example I



www.yafaray.org

alex.v.velikov@gmail.com

Raytracing Example II



www.povray.org

Raytracing Example III



www.yafaray.org

Raytracing Example IV



Summary

- Ray Casting
- Shadow Rays and Local Phong Model
- Reflection
- Transmission

- Next lecture: Geometric queries