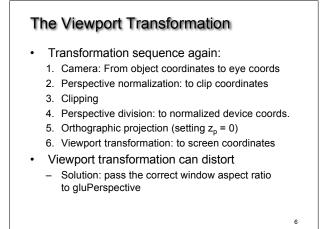
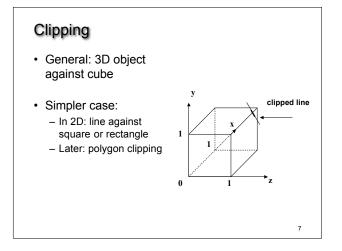
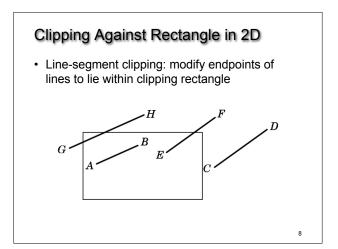


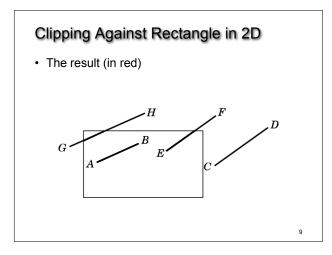


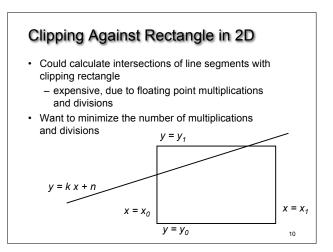
- OpenGL uses $-1 \le x, y, z \le 1$ (others possible)
- · Clip against resulting cube
- Clipping against arbitrary (programmerspecified) planes requires more general algorithms and is more expensive

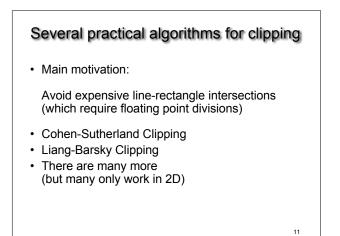


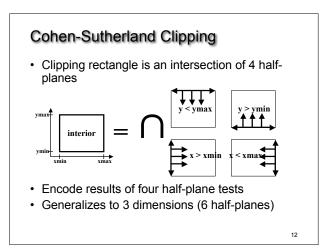


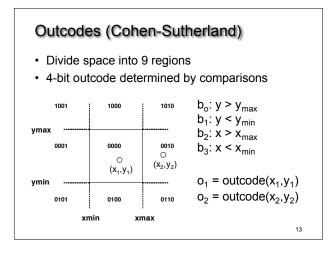


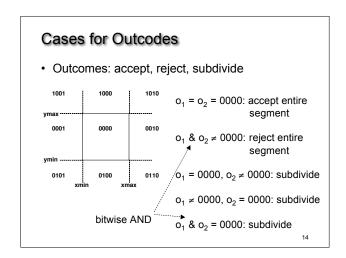












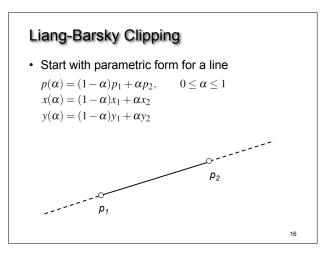
Cohen-Sutherland Subdivision

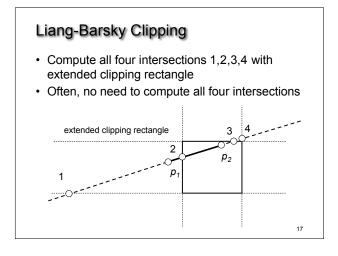
- Pick outside endpoint (o ≠ 0000)
- Pick a crossed edge (o = $b_0b_1b_2b_3$ and $b_k \neq 0$)
- Compute intersection of this line and this edge

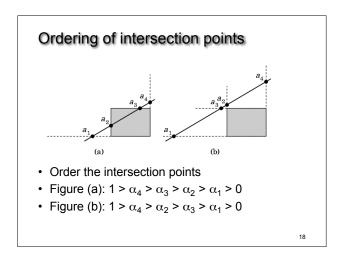
15

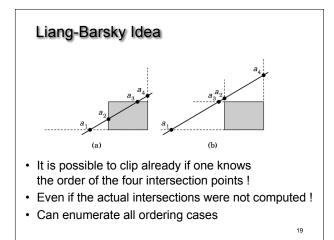
- Replace endpoint with intersection point
- Restart with new line segment

 Outcodes of second point are unchanged
- · This algorithms converges









Liang-Barsky efficiency improvements

- Efficiency improvement 1:
 Compute intersections one by one
 Often can reject before all four are computed
- Efficiency improvement 2:

```
– Equations for \alpha_3, \alpha_2
```

$$y_{\text{max}} = (1 - \alpha_3)y_1 + \alpha_3 y_2$$
$$x_{\text{min}} = (1 - \alpha_2)x_1 + \alpha_2 x_2$$

$$r_{\min} = (1 - \alpha_2)x_1 + \alpha_2 x_2$$

$$\alpha_3 = \frac{y_{\text{max}} - y_1}{y_2 - y_1}$$
 $\alpha_2 = \frac{x_{\text{min}} - x_1}{x_2 - x_1}$

– Compare α_3 , α_2 without floating-point division

Line-Segment Clipping Assessment

- · Cohen-Sutherland
 - Works well if many lines can be rejected early
 - Recursive structure (multiple subdivisions) is
 - a drawback
- Liang-Barsky
 - Avoids recursive calls
 - Many cases to consider (tedious, but not expensive)

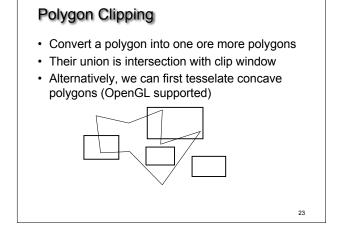
21

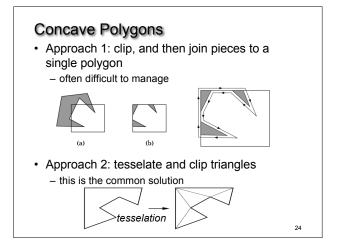
Outline

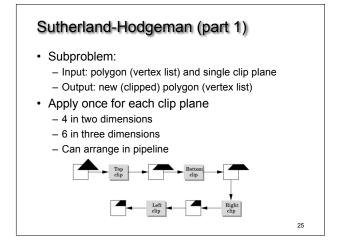
- Line-Segment Clipping
 Cohen-Sutherland
 - Liang-Barsky
- Polygon Clipping

 Sutherland-Hodgeman
- Clipping in Three Dimensions

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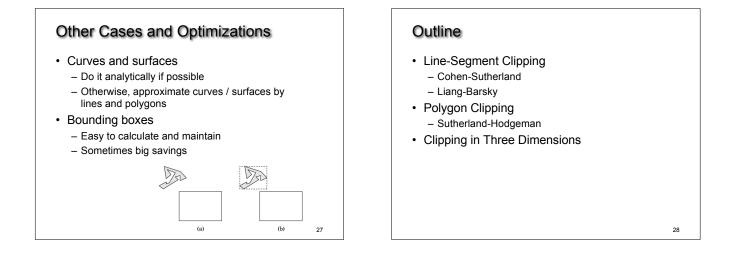


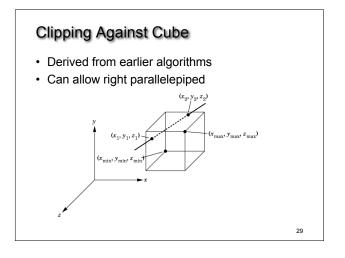


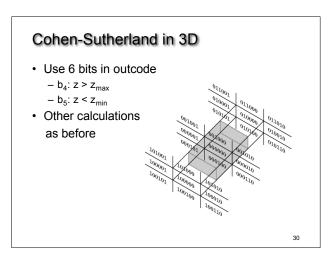


Sutherland-Hodgeman (part 2)

- To clip vertex list (polygon) against a half-plane:
 Test first vertex. Output if inside, otherwise skip.
 - Then loop through list, testing transitions
 - In-to-in: output vertex
 - In-to-out: output intersection
 - out-to-in: output intersection and vertex
 - out-to-out: no output
 - Will output clipped polygon as vertex list
- · May need some cleanup in concave case
- · Can combine with Liang-Barsky idea







Liang-Barsky in 3D

- Add equation $z(\alpha) = (1 \alpha) z_1 + \alpha z_2$
- Solve, for \mathbf{p}_0 in plane and normal \mathbf{n} :

$$p(\alpha) = (1 - \alpha)p_1 + \alpha p_2$$
$$n \cdot (p(\alpha) - p_0) = 0$$

Yields

$$\alpha = \frac{n \cdot (p_0 - p_1)}{n \cdot (p_2 - p_1)}$$

· Optimizations as for Liang-Barsky in 2D

)

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Summary: Clipping

- · Clipping line segments to rectangle or cube - Avoid expensive multiplications and divisions - Cohen-Sutherland or Liang-Barsky
- · Polygon clipping - Sutherland-Hodgeman pipeline
- · Clipping in 3D - essentially extensions of 2D algorithms

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Preview and Announcements

- · Scan conversion
- · Anti-aliasing
- · Other pixel-level operations
- · Assignment 2 due a week from today!
- · Assignment 1 video