CSCI 480 Computer Graphics
Lecture 18

Global Illumination

BRDFs
Raytracing and Radiosity
Subsurface Scattering
Photon Mapping
[Ch. 13.4-13.5]

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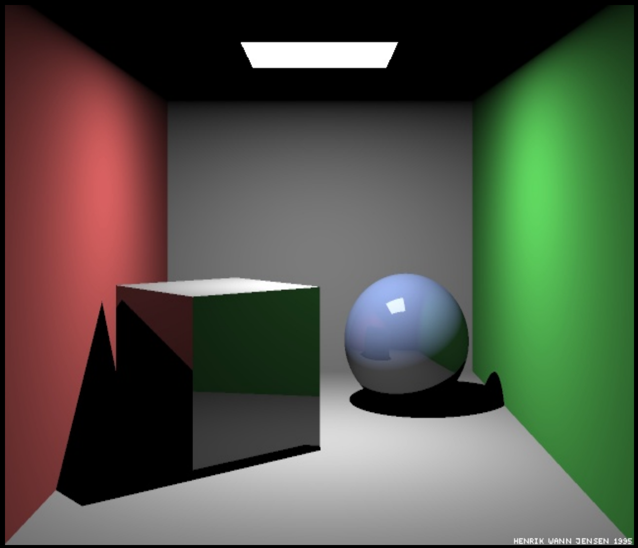
http://www-bcf.usc.edu/~jbarbic/cs480-s12/

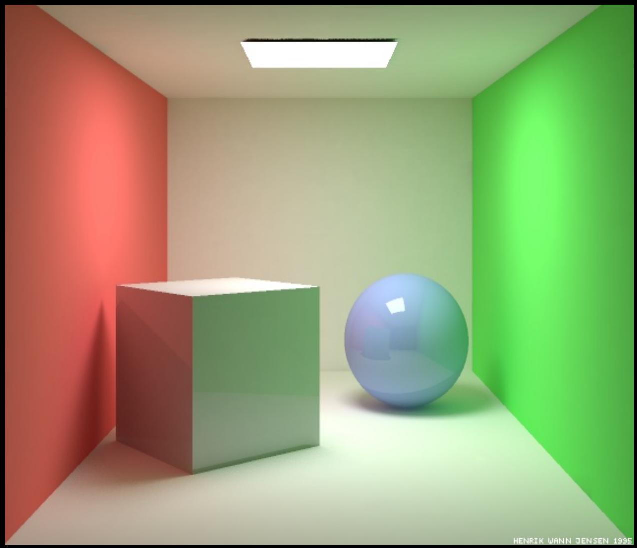
Global Illumination

- Lighting based on the full scene
- Lighting based on physics (optics)
- Traditionally represented by two algorithms
  - Raytracing – 1980
  - Radiosity – 1984
- More modern techniques include *photon mapping* and many variations of raytracing and radiosity ideas

Source: Dianne Hansford,
Arizona State Univ.

Direct Illumination vs. Global Illumination

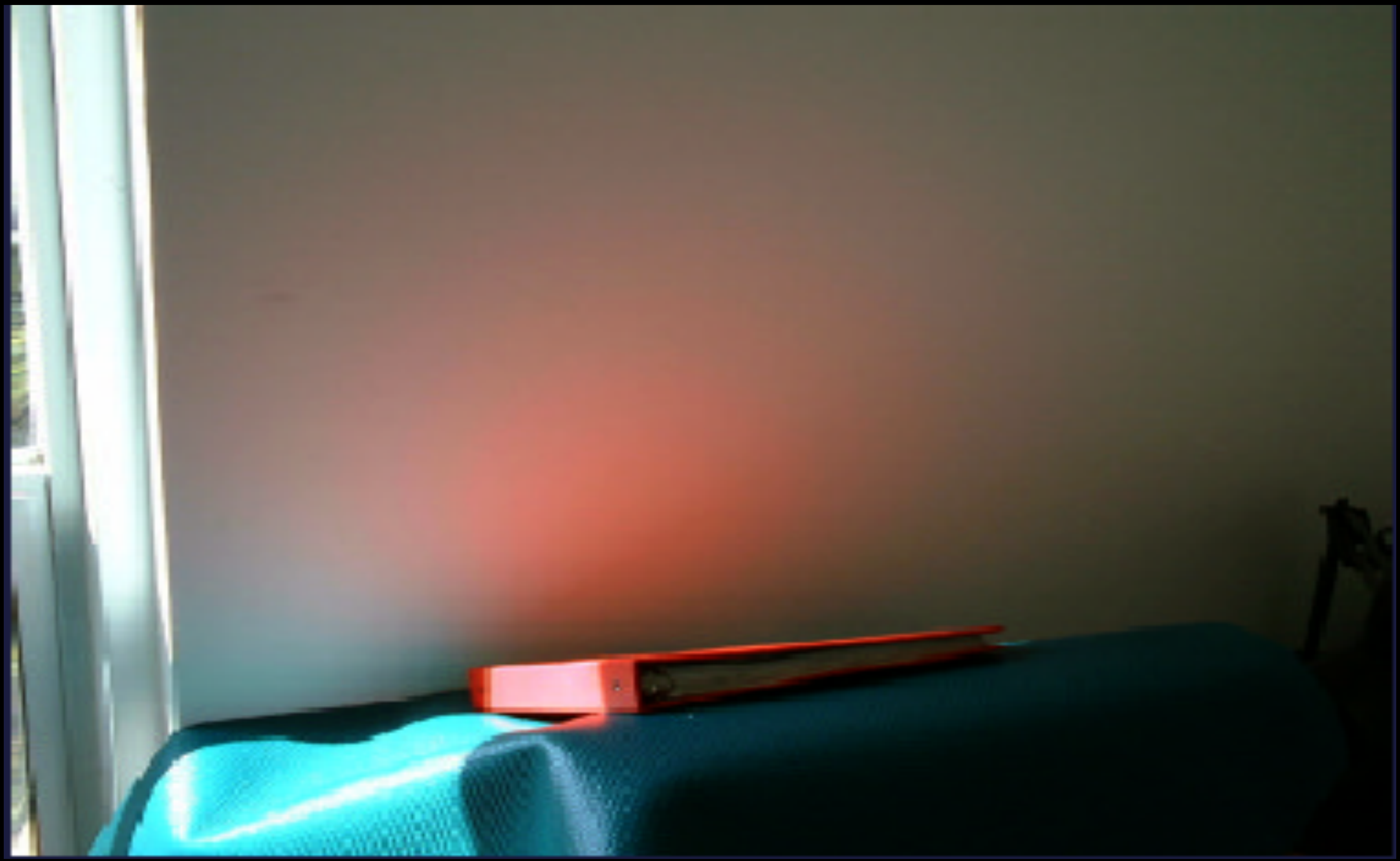




- single (or few) bounces of the light only
- for example, ray casting
- no recursion (or shallow recursion only)
- fast lighting calculations based on light and normal vectors

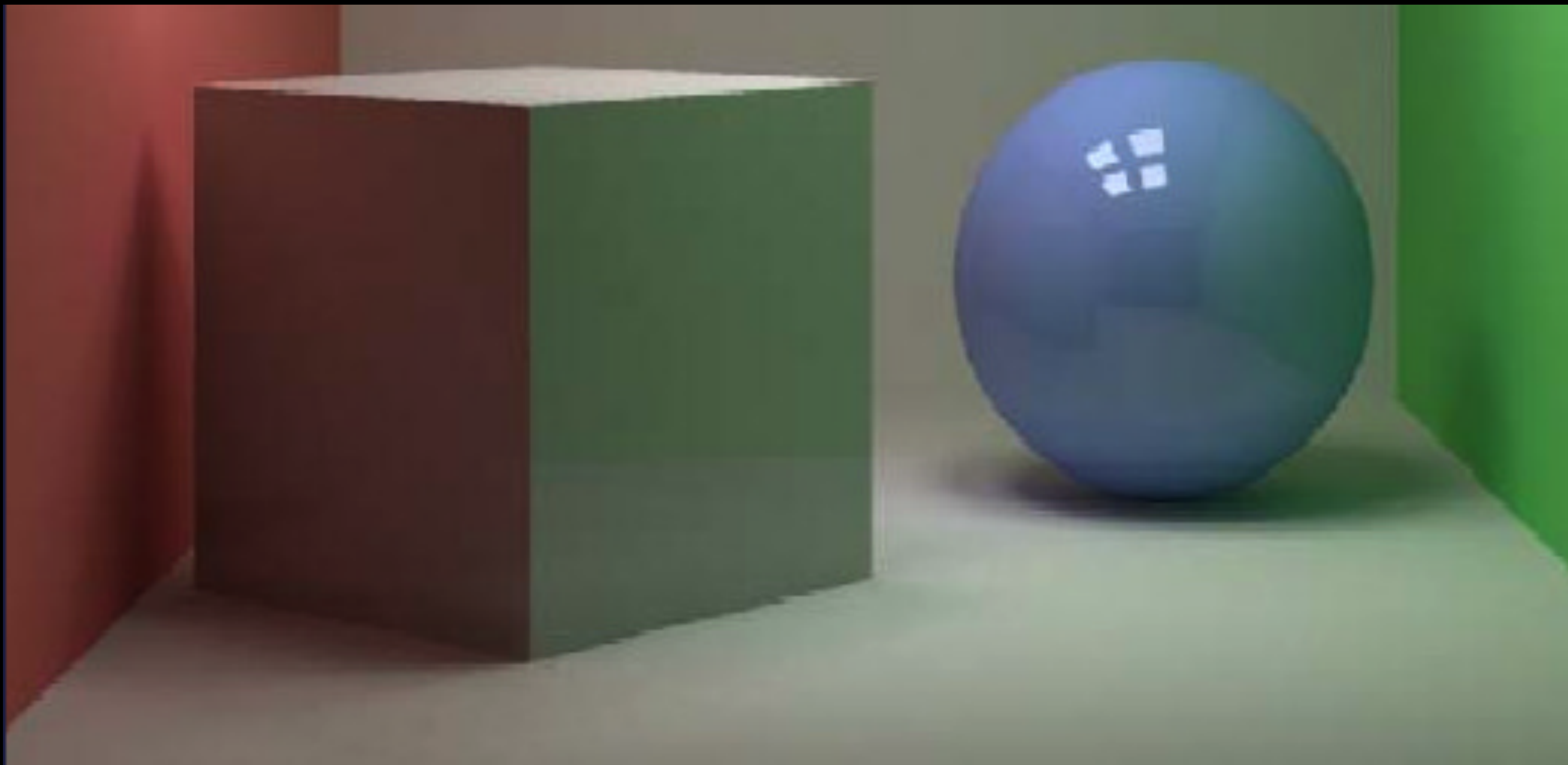
- reflected, scattered and transmitted light
- many (infinite) number of bounces
- physically based light transport

Indirect Illumination



Color Bleeding

Soft Shadows



Shadows are much darker where the direct and indirect illuminations are occluded. Such shadows are important for “sitting” the sphere in the scene. They are difficult to fake without global illumination.

Caustics

- Transmitted light that refocuses on a surface, usually in a pretty pattern

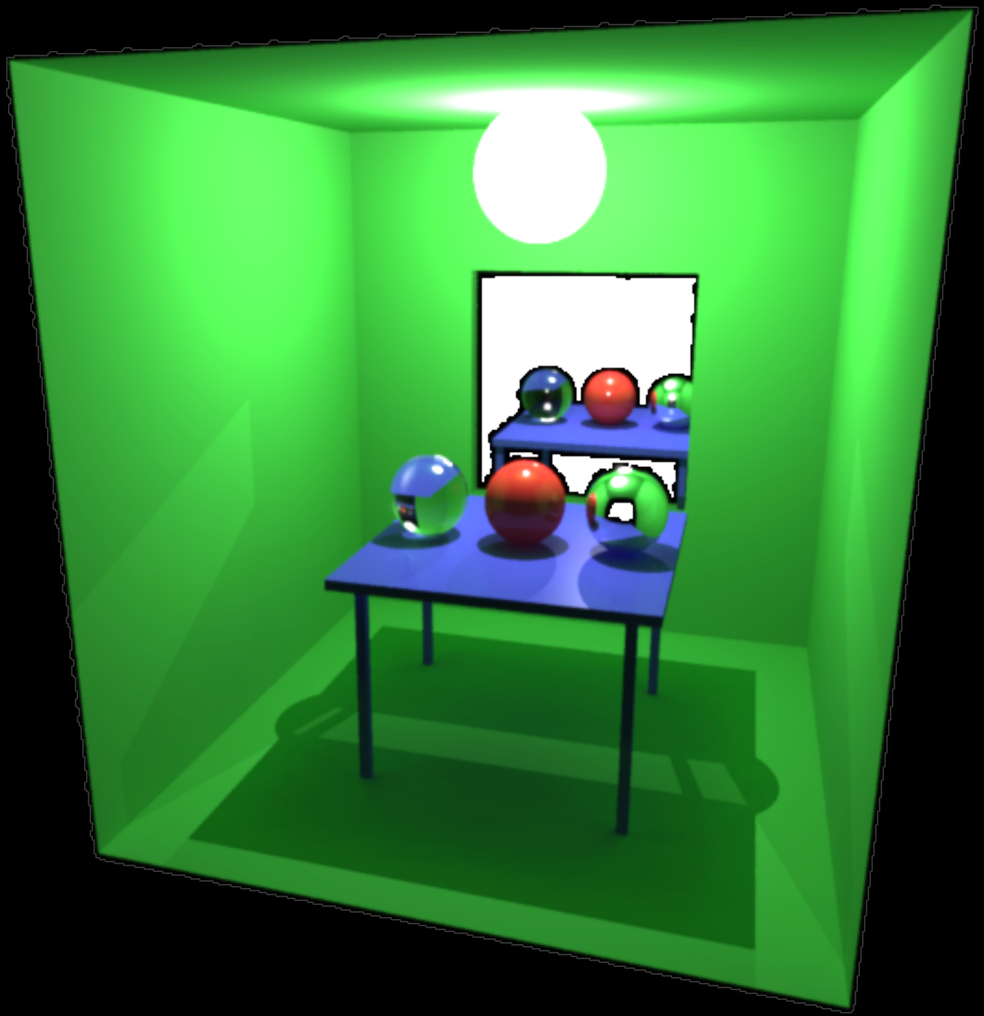
- Not present with direct illumination

Light Transport and Global Illumination

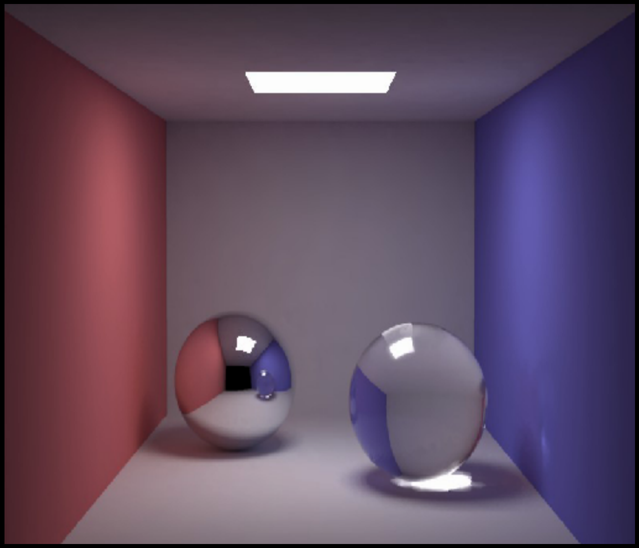
- Diffuse to diffuse
- Diffuse to specular
- Specular to diffuse
- Specular to specular
- Ray tracing (viewer dependent)
  - Light to diffuse
  - Specular to specular
- Radiosity (viewer independent)
  - Diffuse to diffuse

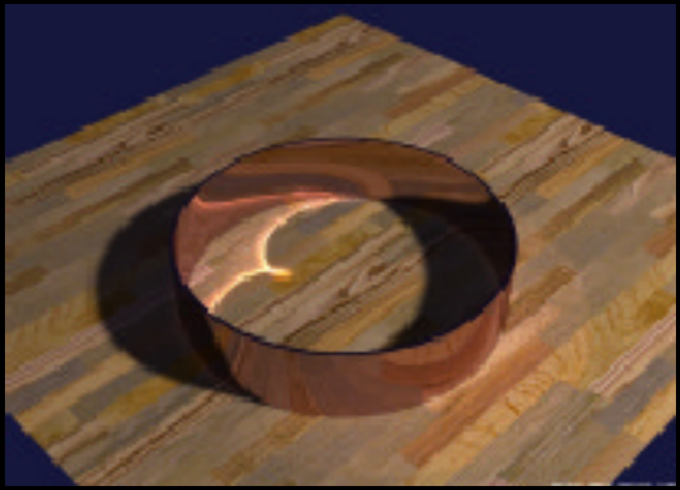
Path Types

- OpenGL
  - L(D|S)E
- Ray Tracing
  - LDS*E
- Radiosity
  - LD*E
- Path Tracing
  - attempts to trace "all rays" in a scene



Images Rendered With Global Illumination





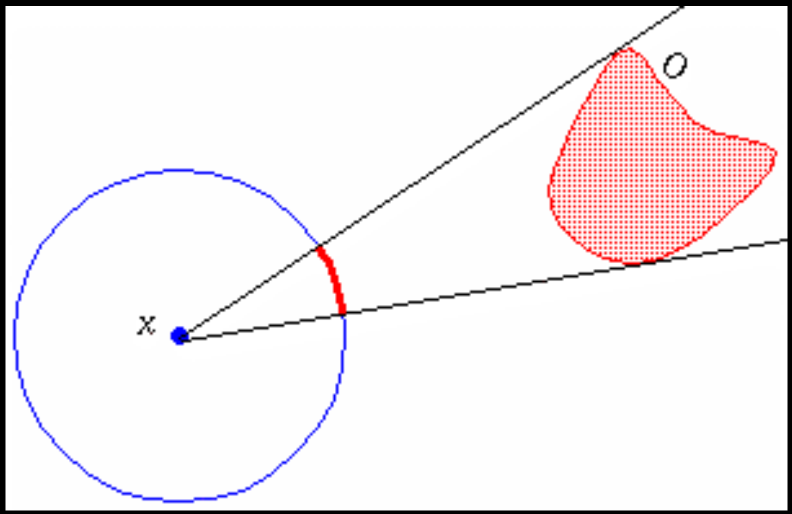
- Caustics
- Color bleeding
- Area light sources and soft shadows

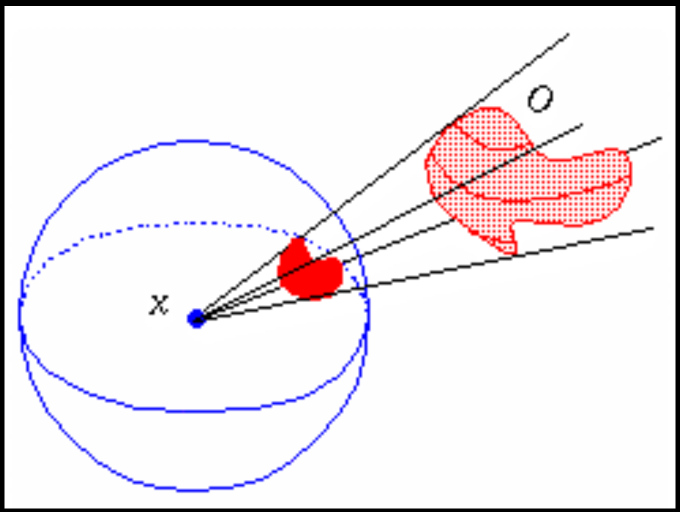
Outline

- Direct and Indirect Illumination
- Bidirectional Reflectance Distribution Function
- Raytracing and Radiosity
- Subsurface Scattering
- Photon Mapping

Solid Angle

- 2D angle subtended by object O from point x:
  - Length of projection onto unit circle at x
  - Measured in radians (0 to 2π)
- 3D solid angle subtended by O from point x:
  - Area of of projection onto unit sphere at x
  - Measured in steradians (0 to 4π)



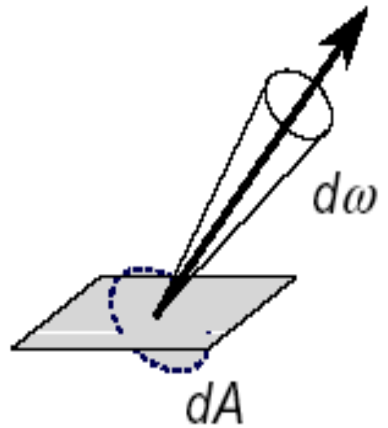


J. Stewart

Light Emitted from a Surface

- Radiance (L): Power (ϕ) per unit area per unit solid angle
  - Measured in W / m^2str
  - *dA is projected area* (perpendicular to given direction)
- Radiosity (B): Radiance integrated over all directions
  - Power from per unit area, measured in W / m^2

$$B = \int_{\Omega} L(\theta, \phi) \cos\theta d\omega$$

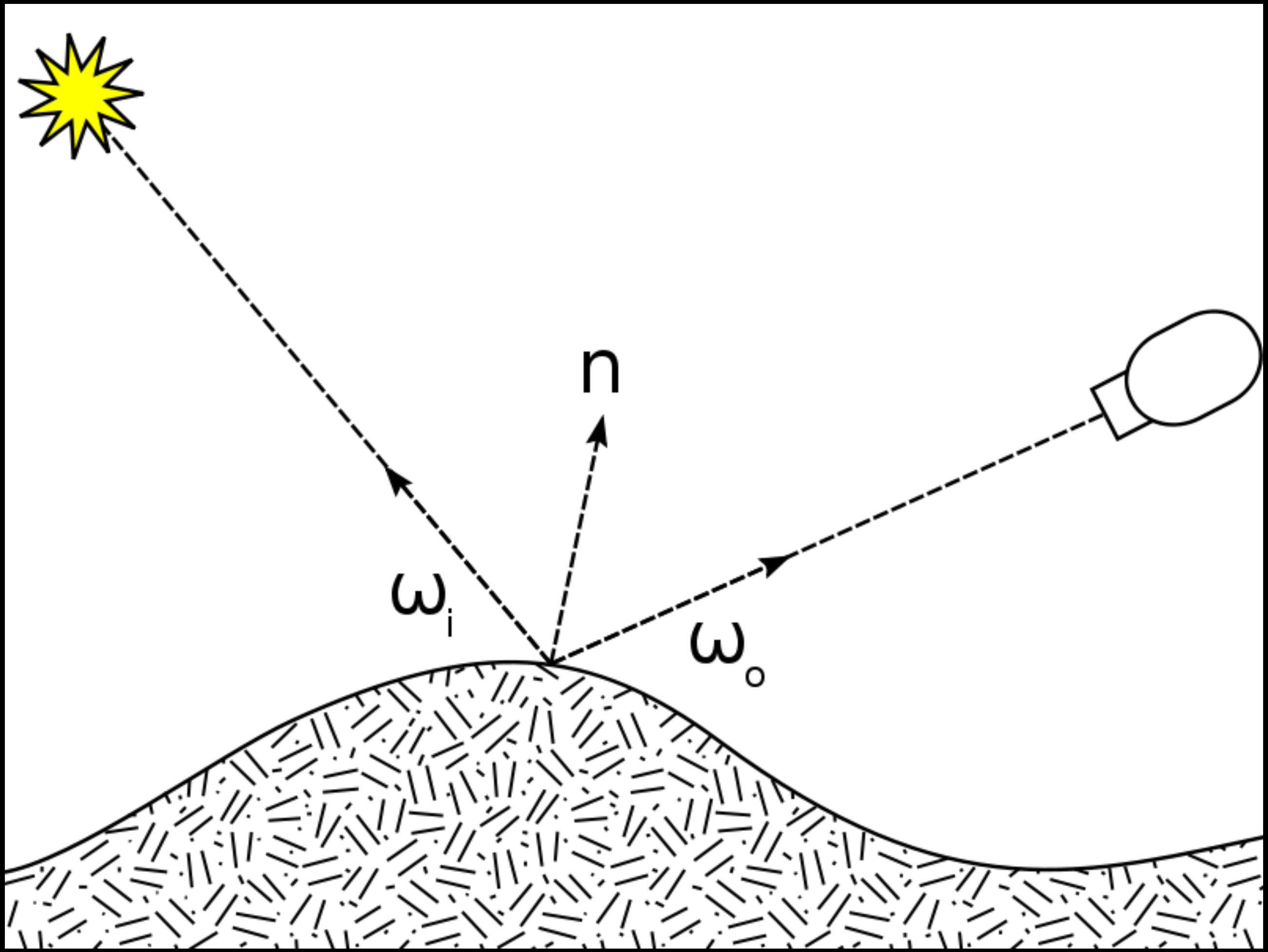


$$L = \frac{d\Phi}{dA\,d\omega}$$

Bidirectional Reflectance Distribution Function (BRDF)

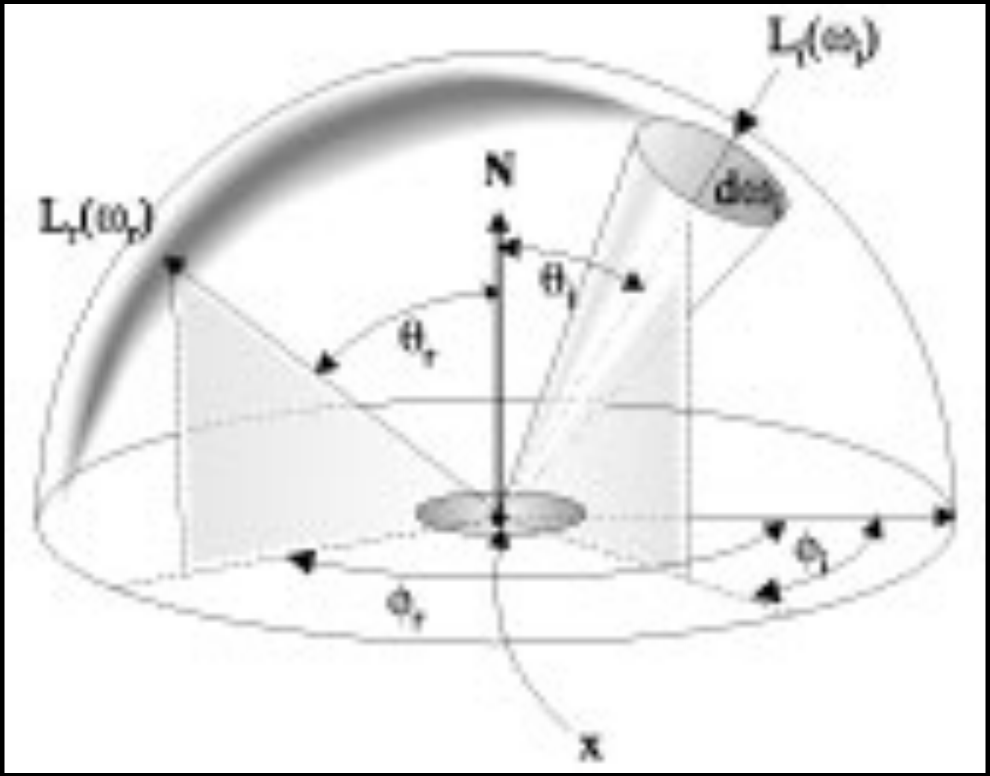
If a ray hits a surface point at angle ω_i, how much light bounces into the direction given by angle ω_o?

It depends on the type of material.



Bidirectional Reflectance Distribution

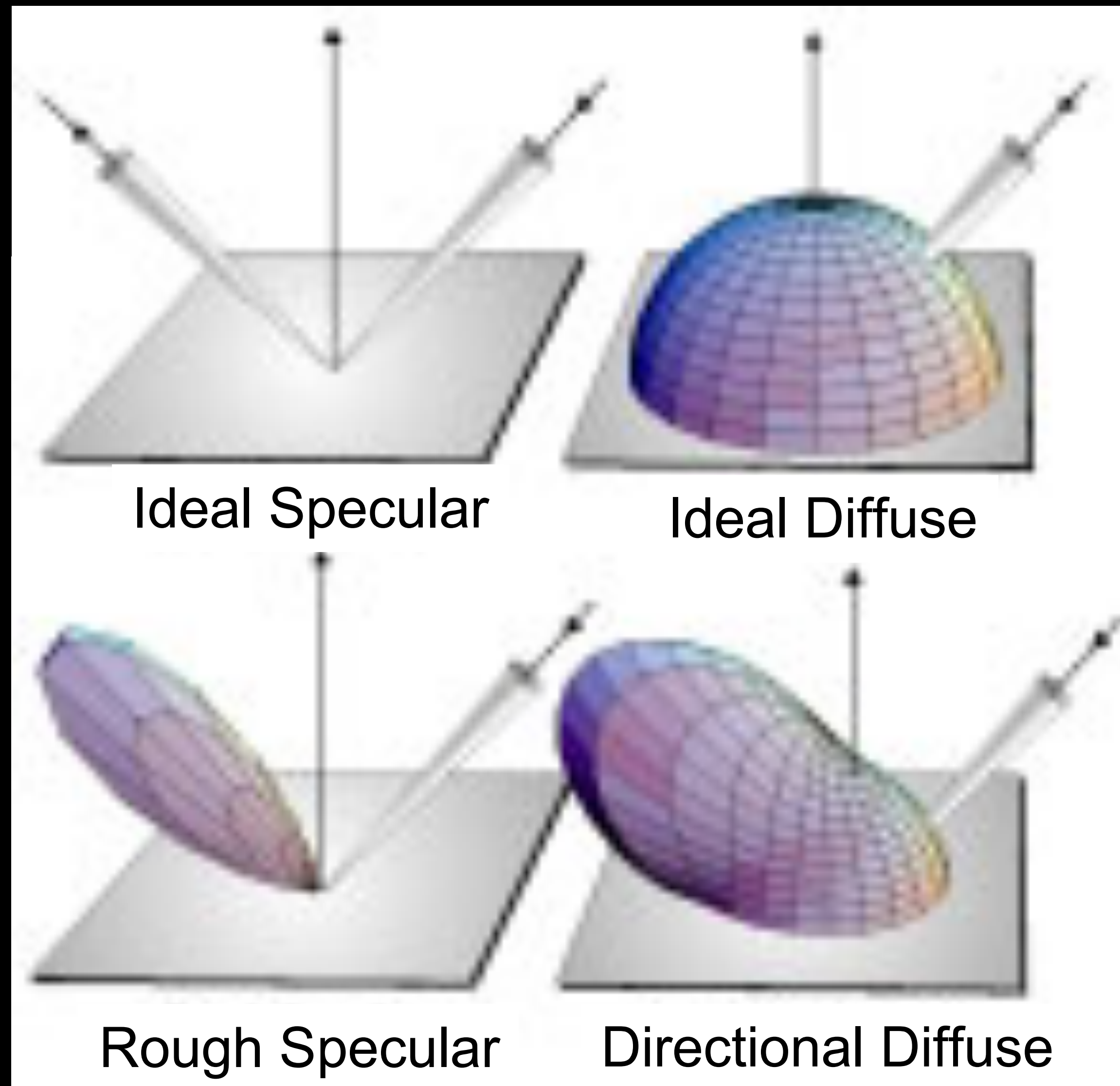
- General model of light reflection
- Hemispherical function
- 6-dimensional (location, 4 angles, wavelength)



A. Wilkie

BRDF Examples

- BRDF is a property of the material
- There is no formula for most materials
- Measure BRDFs for different materials (and store in a table)



Material Examples

Marschner et al. 2000

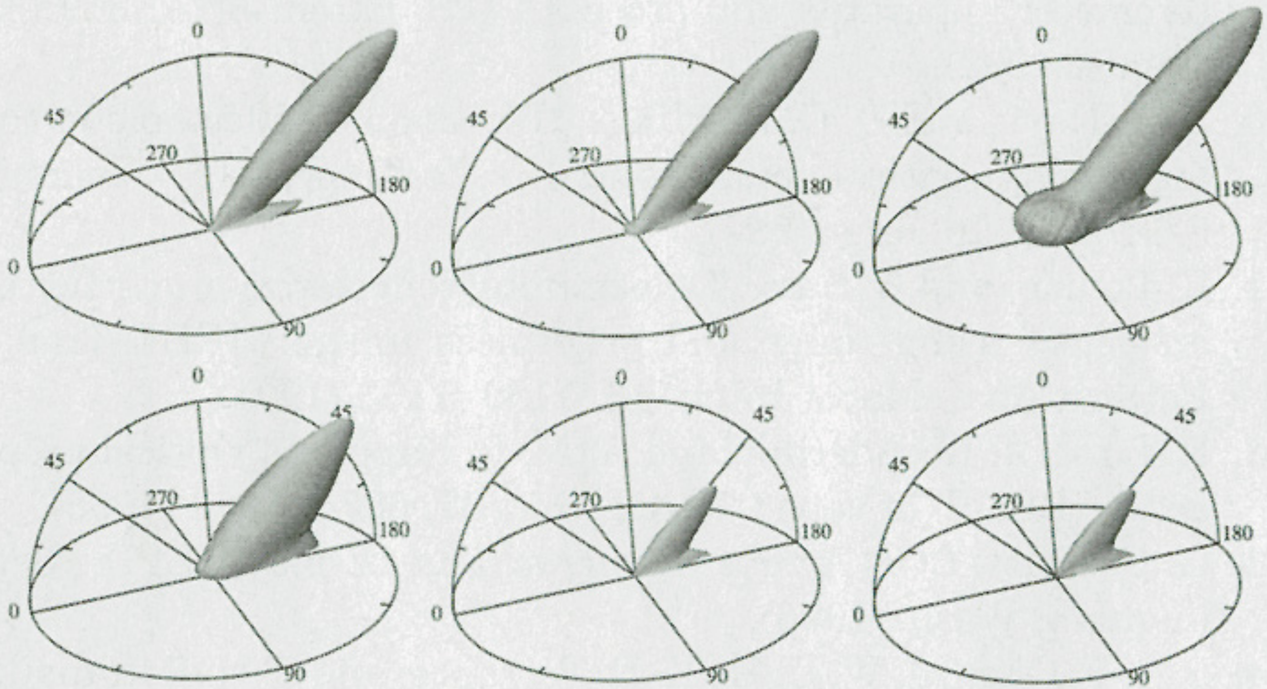


Fig. 16. Resampled scattering diagrams of the BRDF measurements of two paints: a blue enamel (top row) and a red automotive lacquer (bottom row). The RGB color measurements are shown from left to right.

BRDF Isotropy

- Rotation invariance of BRDF
- Reduces 4 angles to 2
- Holds for a wide variety of surfaces
- Anisotropic materials
  - Brushed metal
  - Others?

Rendering Equation

$$L(\mathbf{x},\omega) = E(\mathbf{x},\omega) + \int f_r(\mathbf{x},\omega,\omega')G(\mathbf{x},\mathbf{x}')V(\mathbf{x},\mathbf{x}')L(\mathbf{x}',\omega')dA'$$

- *L* is the radiance from a point on a surface in a given direction *ω*
- *E* is the emitted radiance from a point: *E* is non-zero only if *x*' is emissive
- *V* is the visibility term: 1 when the surfaces are unobstructed along the direction *ω*, 0 otherwise
- *G* is the geometry term, which depends on the geometric relationship between the two surfaces *x* and *x*'
- It includes contributions from light bounced many times off surfaces
- f_r is the BRDF

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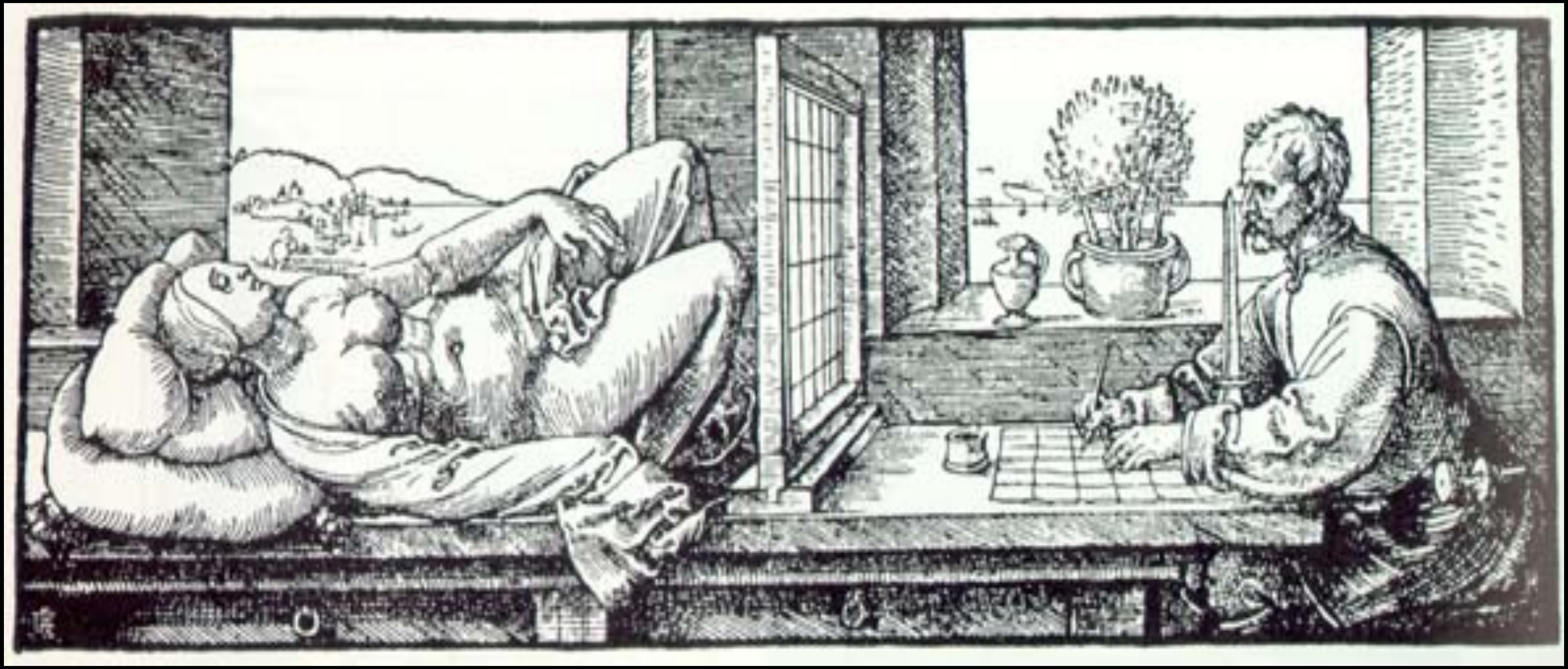
Raytracing

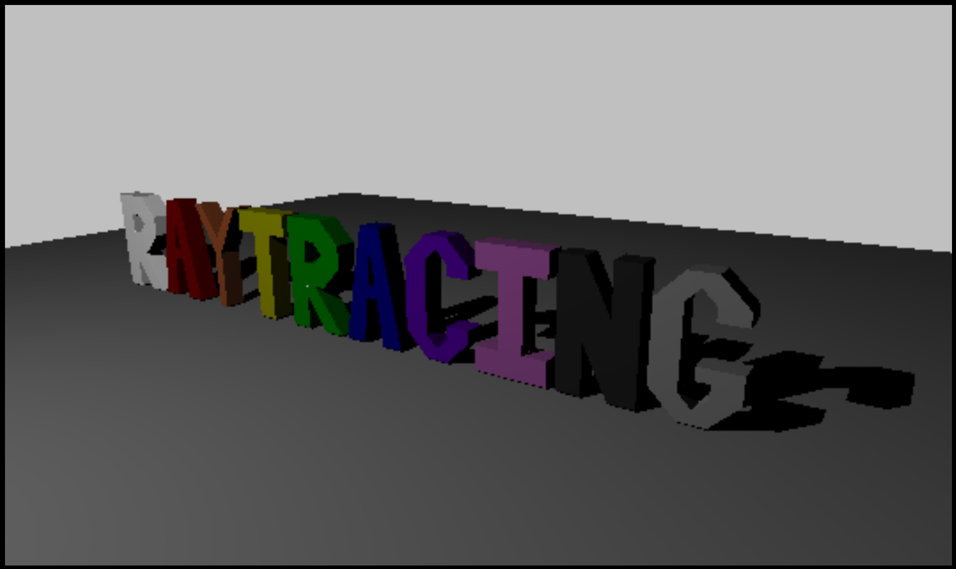
From: http://jedi.ks.uiuc.edu/~johns/raytracer/raygallery/stills.html

Raytracing

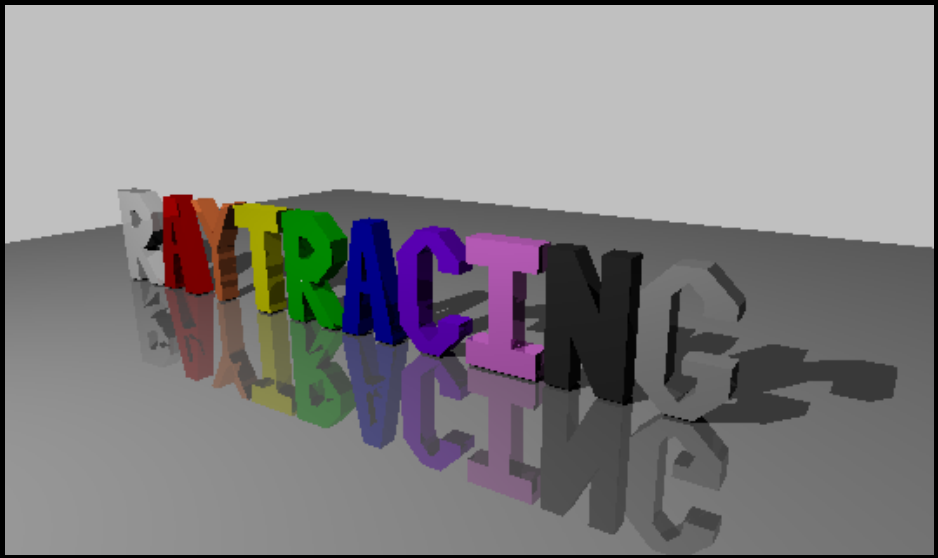


Albrecht Duerer,
Underweysung der Messung mit dem Zirkel und Richtscheyt
(Nurenberg, 1525), Book 3, figure 67.

Raycasting vs. Raytracing



Raycasting



Raytracing

Raytracing: Pros

- Simple idea and nice results
- Inter-object interaction possible
  - Shadows
  - Reflections
  - Refractions (light through glass, etc.)
- Based on real-world lighting

Raytracing: Cons

- Slow
- Speed often highly scene-dependent
- Lighting effects tend to be abnormally sharp, without soft edges, unless more advanced techniques are used
- Hard to put into hardware

Supersampling I

- Problem: Each pixel of the display represents one single ray
  - Aliasing
  - Unnaturally sharp images

- Solution: Send multiple rays through each "pixel" and average the returned colors together

Supersampling II

- Direct supersampling
  - Split each pixel into a grid and send rays through each grid point
- Adaptive supersampling
  - Split each pixel only if it's significantly different from its neighbors
- Jittering
  - Send rays through randomly selected points within the pixel

The Radiosity Method

Cornell University

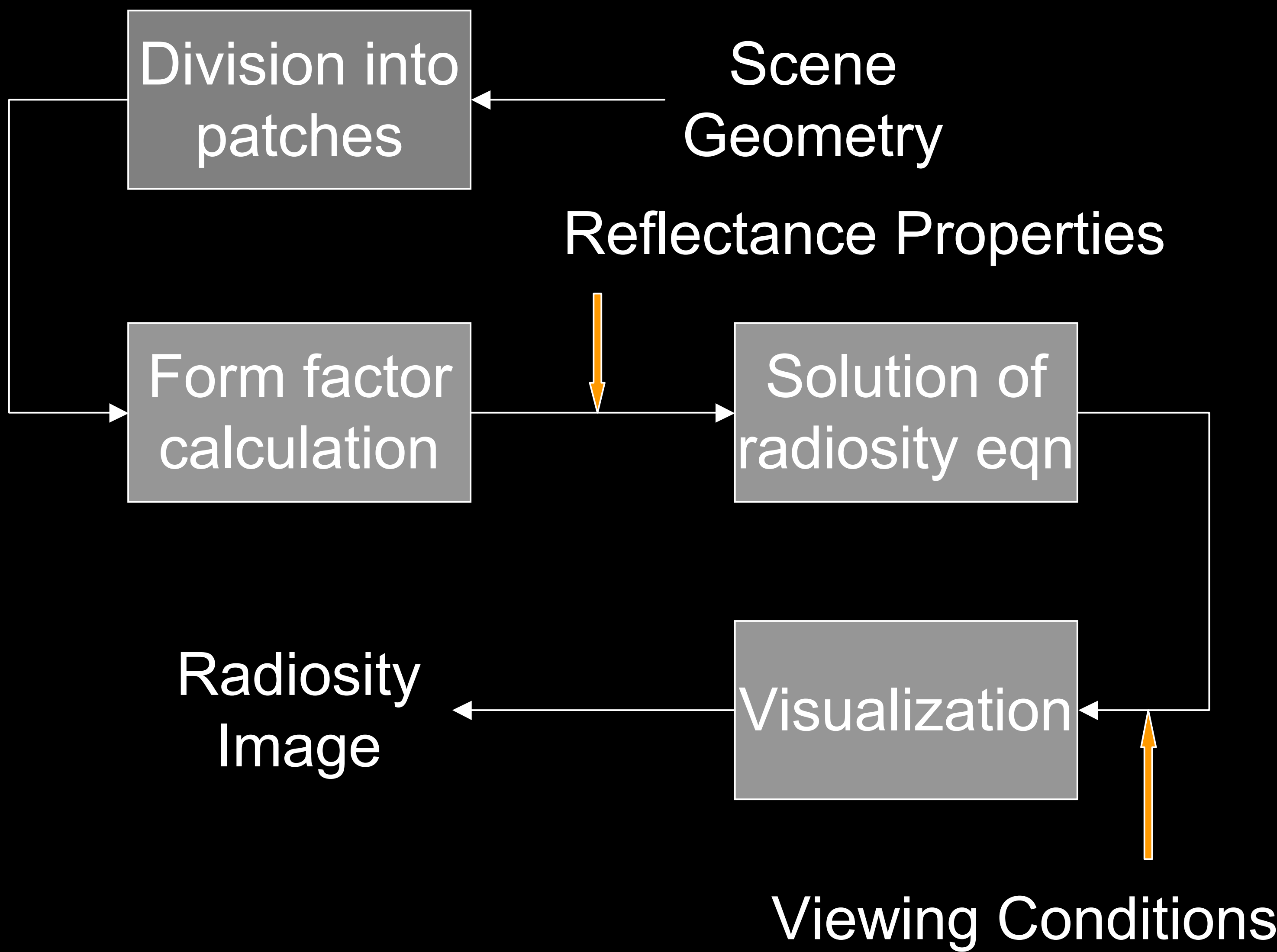
The Radiosity Method

- Divide surfaces into patches
  (e.g., each triangle is one patch)

- Model light transfer between patches as system of linear equations

- Important assumptions:
  - **Diffuse reflection only**
  - No specular reflection
  - No participating media (no fog)
  - No transmission (only opaque surfaces)
  - Radiosity is constant across each patch
  - Solve for R, G, B separately

(Idealized) Radiosity Computation



Radiosity: Pros

- Viewpoint independence means fast real-time display after initial calculation
- Inter-object interaction possible
  - Soft shadows
  - Indirect lighting
  - Color bleeding
- Accurate simulation of energy transfer

Radiosity: Cons

- Precomputation must be re-done if *anything* moves
- Large computational and storage costs
- Non-diffuse light not represented
  - Mirrors and shiny objects hard to include
- Lighting effects tend to be “blurry” (not sharp)
- Not applicable to procedurally defined surfaces

Radiosity Equation

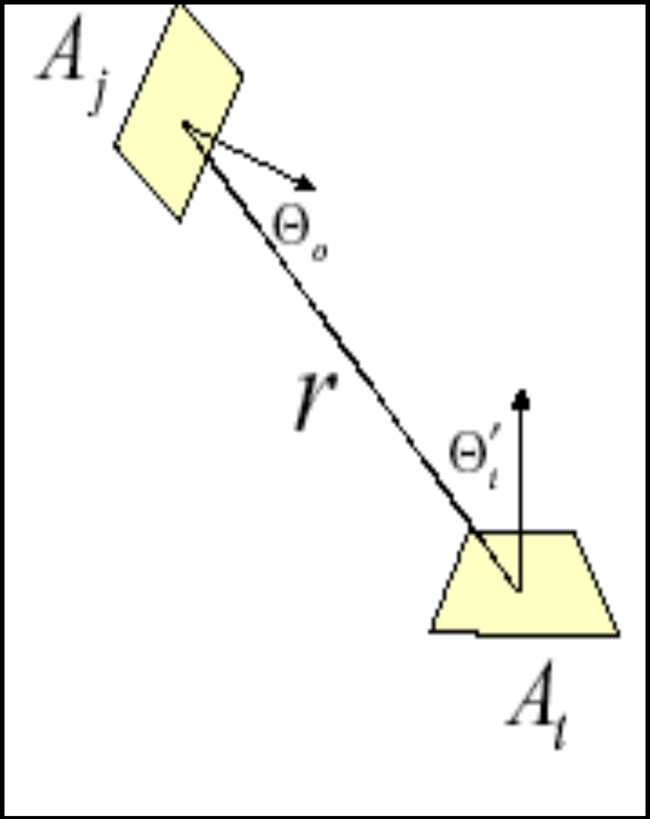
- For each patch i:

$$
\begin{aligned}
B_i &= E_i + \rho_i \sum_j (F_{ji} A_j / A_i) B_j \\
&= E_i + \rho_i \sum_j F_{ij} B_j
\end{aligned}
$$

- Variables
  - B_i = radiosity (unknown)
  - E_i = emittance of light sources (given; some patches are light sources)
  - ρ_i = reflectance (given)
  - F_{ij} = form factor from i to j (computed)
    fraction of light emitted from patch i arriving at patch j
  - A_i = area of patch i (computed)

The Form Factor

$$F_{ij} = \frac{1}{A_i} \int_{A_i} \int_{A_j} \frac{V_{ij} \cos\phi_i \cos\phi_j}{\pi r^2} dA_j dA_i$$



F_{ij} is dimensionless

V_{ij} = 0 if occluded
1 if not occluded
(visibility factor)

Radiosity Example

Museum simulation. Program of Computer Graphics, Cornell University. 50,000 patches. Note indirect lighting from ceiling.

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Subsurface Scattering

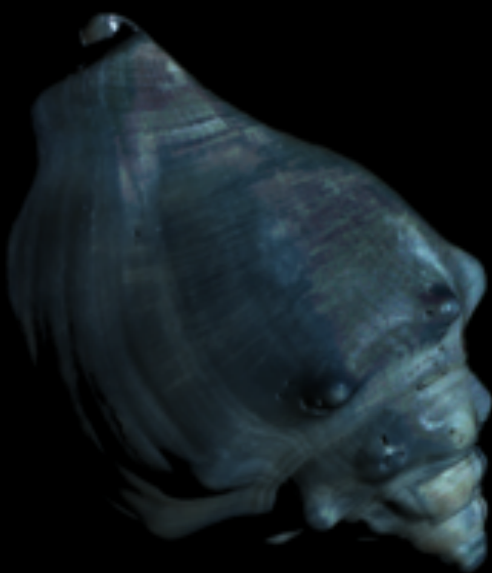
- Translucent objects: skin, marble, milk
- Light penetrates the object, scatters and exits
- Important and popular in computer graphics

Subsurface Scattering

- Jensen et al. 2001

Using only BRDF — With subsurface light transport

Subsurface Scattering



direct only

subsurface scattered only

combined

Source: Wikipedia

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Photon Mapping

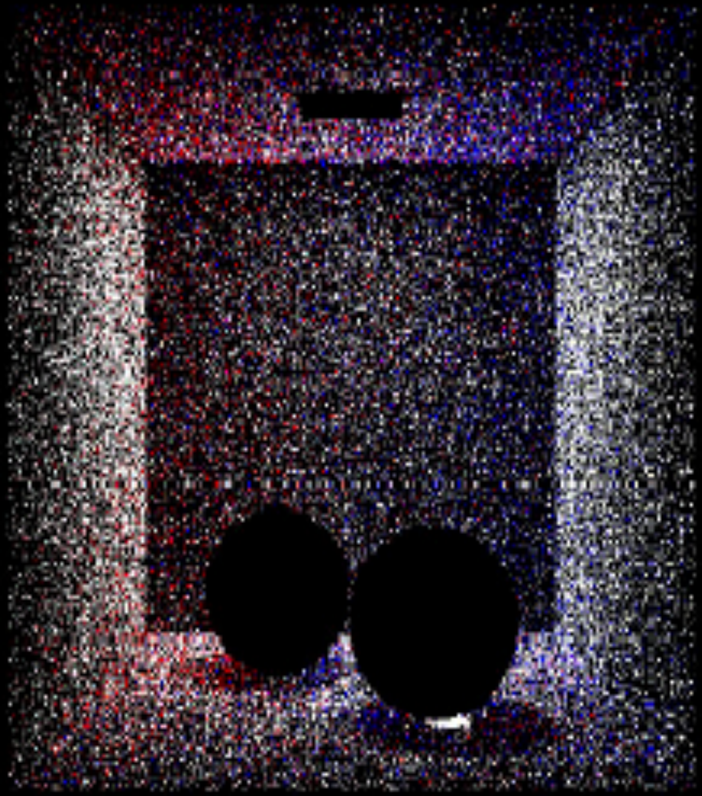
From http://graphics.ucsd.edu/~henrik/images/global.html

Photon Mapping Basics

- Enhancement to raytracing
- Can simulate caustics
- Can simulate diffuse inter-reflections
(e.g., the "bleeding" of colored light from a red wall onto a white floor, giving the floor a reddish tint)
- Can simulate clouds or smoke

Photon Mapping

- "Photons" are emitted (raytraced) from light sources
- Photons either bounce or are absorbed
- Photons are stored in a *photon map,* with both position and incoming direction
- Photon map is decoupled from the geometry (often stored in a kd-tree)



Photon Map

Photon Mapping

- Raytracing step uses the closest *N* photons to each ray intersection and estimates the outgoing radiance
- Specular reflections can be done using “usual” raytracing to reduce the number of photons needed
- Numerous extensions to the idea to add more complex effects

Photon Mapping: Pros

- Preprocessing step is view independent, so only needs to be re-done if the lighting or positions of objects change
- Inter-object interaction includes:
  - Shadows
  - Indirect lighting
  - Color bleeding
  - Highlights and reflections
  - Caustics – *current method of choice*
- Works for procedurally defined surfaces

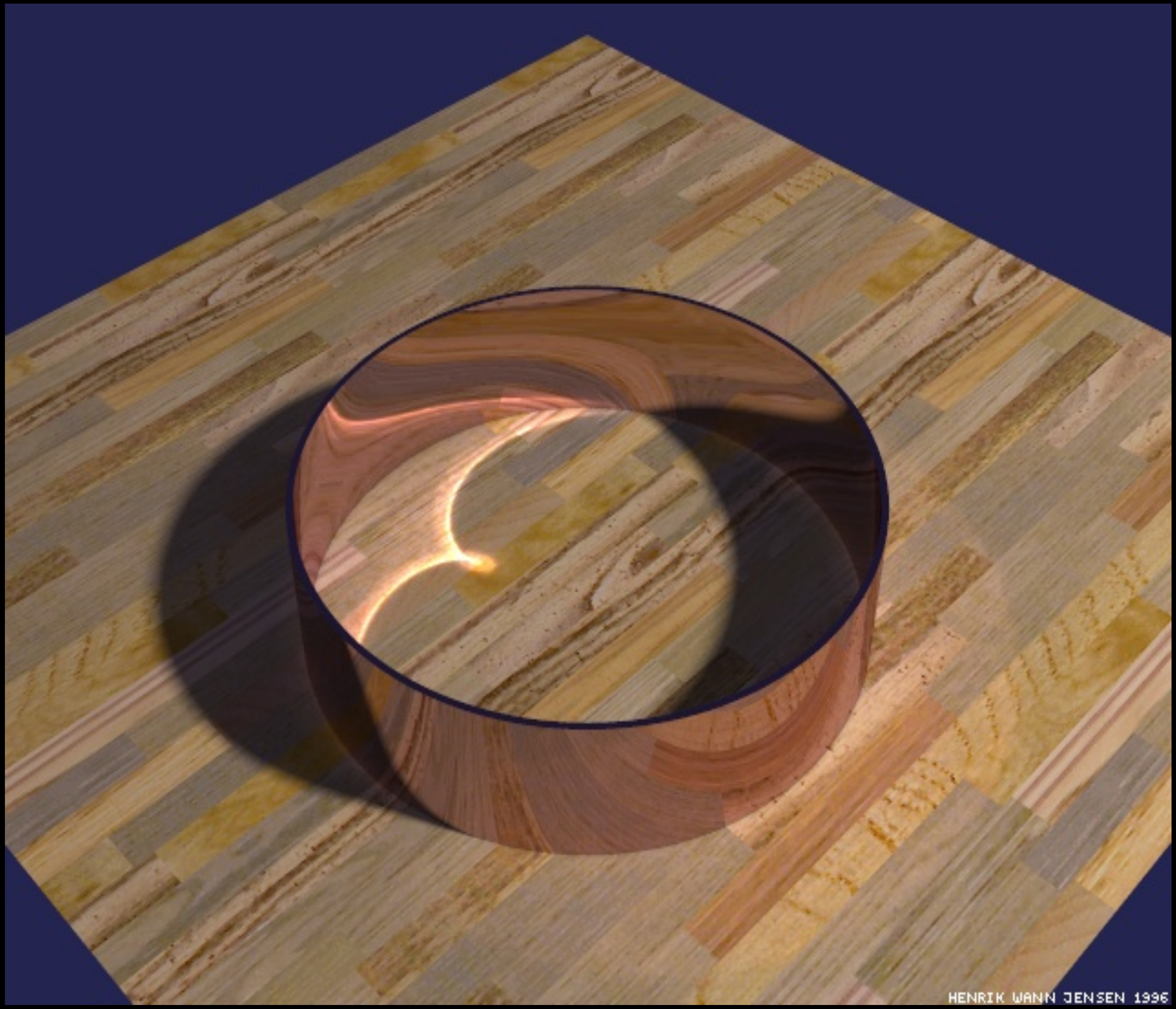
Photon Mapping: Cons

- Still time-consuming, although not as bad as comparable results from pure raytracing
- Photon map not easy to update if small changes are made to the scene

Photon Mapping Example

224,316 caustic photons, 3095 global photons

Photon Mapping Example



Summary

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